

# Nuclear Level Density and $\gamma$ -ray Strength Function of $^{67}\text{Ni}$ and the impact on the $i$ -process

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Proton- $\gamma$  coincidences from (d, p) reactions between a  $^{66}\text{Ni}$  beam and a deuterated polyethylene target have been analyzed with the inverse Oslo method to find the nuclear level density (NLD) and  $\gamma$ -ray strength function ( $\gamma\text{SF}$ ) of  $^{67}\text{Ni}$ . The  $^{66}\text{Ni}(n, \gamma)$  capture cross section has been calculated using the Hauser-Feshbach model in TALYS using the measured NLD and  $\gamma\text{SF}$  as constraints. We confirm that  $^{66}\text{Ni}(n, \gamma)$  acts as a bottleneck when relying on one-zone nucleosynthesis calculations. However, we find that the impact of this reaction is strongly damped in multi-zone low-metallicity AGB stellar models experiencing  $i$ -process nucleosynthesis.

## I. INTRODUCTION

The origin and production mechanism of the heavy elements has been under investigation for a long time. The first direct observations of nucleosynthesis of heavy elements was reported by P. Merrill in 1952 [1]. Soon after, the mechanism behind the production of heavy elements through neutron capture was outlined in the famous B<sup>2</sup>FH paper in 1957 [2].

Nucleosynthesis beyond the Fe/Ni mass region is due to the slow neutron capture (s-process), rapid neutron capture (r-process), photo-disintegration processes, and

more recent results call for an intermediate neutron capture process ( $i$ -process) [3, 4]. These processes are sensitive to nuclear properties such as the nuclear level densities (NLD) and  $\gamma$ -ray strength functions ( $\gamma\text{SF}$ ). The availability and uncertainties in nuclear data affect the ability to calculate reaction rates, in particular for the  $r$ - and  $i$ -processes as they involve neutron-rich nuclei for which data is non-existing or sparse. This can have significant impact on the neutron capture rates and on the final abundance distribution of elements and their isotopes predicted by models. Currently, the vast majority of nuclei for which NLDs and  $\gamma\text{SF}$ s have been measured lie at, or very near, the line of stability [5].

Away from stability, directly measured ( $n, \gamma$ ) cross sections are not available and NLDs and  $\gamma\text{SF}$ s can provide the necessary constraints. The Oslo method is particularly suitable as it extracts NLD and  $\gamma\text{SF}$  simultaneously [6, 7]. These quantities, together with the optical model potentials, are the main ingredients in the *Hauser-Feshbach* theory [8] to calculate neutron capture cross-sections and reaction rates. The Oslo Method has been further developed using total absorption spectroscopy following  $\beta$ -decay leading to the  $\beta$ -Oslo method [9] and has demonstrated the versatility of the Oslo method and its

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applicability even for nuclei far from stability [9–13]. The  $\beta$ -Oslo method requires specific  $\beta$ -Q value conditions for the mother-daughter pair placing a limit on the nuclei which can be measured with this technique.

Another approach is to use inverse kinematics with radioactive beams. Here the beam intensity is the main limiting factor. Applying the Oslo method to experimental data from an inverse kinematics experiment was first demonstrated in Ref. [14] extracting the NLD and  $\gamma$ SF of  $^{87}\text{Kr}$  following a  $d(^{86}\text{Kr}, p)^{87}\text{Kr}$  pick-up reaction. In this paper, we have applied this inverse-Oslo method to data from a radioactive ion beam experiment to extract the NLD and  $\gamma$ SF of  $^{67}\text{Ni}$ . Based on these results, the neutron capture rate of  $^{66}\text{Ni}$  was constrained using the Hauser-Feshbach theory, which is of particular importance for our understanding of the weak  $i$ -process. In the weak  $i$ -process the neutron density is large ( $\sim 10^{15}$ ), but exposure is low due to a quick and abrupt termination of the neutron production. In such a case only the first  $n$ -capture peak elements are produced significantly [15]. This was studied in Ref. [15], where it was found that the  $^{66}\text{Ni}(n, \gamma)$  reaction had a major impact on the overall production rate of heavier elements, essentially acting as a bottleneck for the entire weak  $i$ -process. Constraining the  $^{66}\text{Ni}(n, \gamma)$  could improve our understanding of the  $i$ -process nucleosynthesis.

## II. EXPERIMENT AND ANALYSIS

The experiment was performed using the HIE-ISOLDE facility at CERN [16], where 1.4 GeV proton beam from the PSBooster bombarded a uranium carbide target inducing fission. The evaporated fission products were ionized by the resonance ionization laser ion source (RILIS) [17] and the  $^{66}\text{Ni}$  ions were separated by the General Purpose Separator (GPS) to be collected and cooled by a penning trap (REXTRAP) [18]. The ions were then charge braid to a  $16^+$  charge state by an electron-beam ion source (REXEBS) [19, 20]. The highly ionized  $^{66}\text{Ni}$  ions were re-accelerated by the HIE-ISOLDE linear accelerator to an energy of 4.47(1) MeV/u. The  $\approx 3.5 \times 10^6$  pps intense  $^{66}\text{Ni}$  beam impinged on a  $\approx 670 \mu\text{g}/\text{cm}^2$  thick secondary deuterated polyethylene target (99 % enrichment in deuterium) [21] placed at the Miniball experimental station and produced the desired  $d(^{66}\text{Ni}, p)^{67}\text{Ni}$  reactions. The total time of beam on target was approximately 140 hours. The same reaction has previously been measured at ISOLDE by Ref. [22], but used a much lower beam energy of 2.5 MeV/u. The data-set was not considered as it only reached excitation energies up to 3.5 MeV, much less than what is required for the Oslo Method.

Protons from the reaction were measured with the C-REX particle detector array [23]. Coincident  $\gamma$ -rays were measured using the Miniball detector array [24, 25]. Two of the eight Miniball high-purity germanium (HPGe) clusters [25] were replaced by six large-volume ( $3.5 \times 8$  inch)  $\text{LaBr}_3:\text{Ce}$  detectors to increase the high  $\gamma$ -ray en-

ergy efficiency of the array. Signals from the C-REX detectors were processed by an analog data acquisition system (DAQ) which fed four 32-channel analogue-to-digital converter (ADC) modules from Mesytec. The signals from the  $\gamma$ -ray detectors were processed by a digital DAQ consisting of XIA Digital Gamma Finders (DGF-4C). The two systems were synchronized, read out simultaneously and the data written to disk.

Prompt particle- $\gamma$  coincidences were selected from the data by applying time gates on the time difference between the detected  $\gamma$ -rays and particles, while the  $(d, p)$  reaction was selected by applying the appropriate energy cut on the  $\Delta E - E$  matrix. Background events were selected in a similar fashion by placing time gates of half the size as the prompt gate on either sides of the prompt peak. This resulted in a total of  $3.2 \times 10^5$  and  $1.1 \times 10^6$  background subtracted proton- $\gamma$  coincidences with the  $\text{LaBr}_3:\text{Ce}$  detectors and the Miniball clusters, respectively. The low number of proton- $\gamma$  coincidences with the  $\text{LaBr}_3:\text{Ce}$  compared to those with the Miniball detectors is due to the lower geometric efficiency of the  $\text{LaBr}_3:\text{Ce}$  detectors which were located considerably further from the target. Although having only a quarter of the Miniball coincidences, the significantly higher full-energy efficiency of the  $\text{LaBr}_3:\text{Ce}$  include the majority of high-energy  $\gamma$ -ray transitions. For this reason, the results presented here are based on the analysis of proton- $\gamma$  coincident events from the  $\text{LaBr}_3:\text{Ce}$  detectors only.

Due to the considerable residual kinetic energy of the  $^{67}\text{Ni}$  the  $\gamma$ -ray energies were Doppler corrected. The maximum deflection of the residual  $^{67}\text{Ni}$  was less than  $1.5^\circ$  and the maximum spread in velocity was less than 4.2% and the correction was performed using a constant factor based only on the  $\gamma$ -detector angle relative to the beam axis.

For each proton- $\gamma$  event the excitation energy was calculated from the kinematic reconstruction of the two-body reaction. The proton- $\gamma$  coincidences were collected in an excitation- $\gamma$  energy matrix shown in Fig. 1(a).

Due to the Lorentz boost associated with inverse-kinematics there were no well resolved levels in the particle spectra suitable for an in-beam calibration. The particle spectra were calibrated through the gain and shift parameters which were found by performing a least squares fit of the entire  $\Delta E - E$  matrix to theoretical particle energies based on the detector thickness. The calibration parameters yielded by this procedure were less precise and contributes significantly to the reduced excitation energy resolution seen in Fig. 1, although the actual contribution due to the calibration is difficult to quantify.

The first step to obtain NLDs and  $\gamma$ SFs from excitation- $\gamma$  matrices is to correct for the detector response using the unfolding method [26] by using a detector response deduced from a Geant4 [27] simulation of the experimental setup [28]. This resulted in the *unfolded* matrix shown in Fig. 1(b).

Next, an iterative subtraction method [29] is applied to

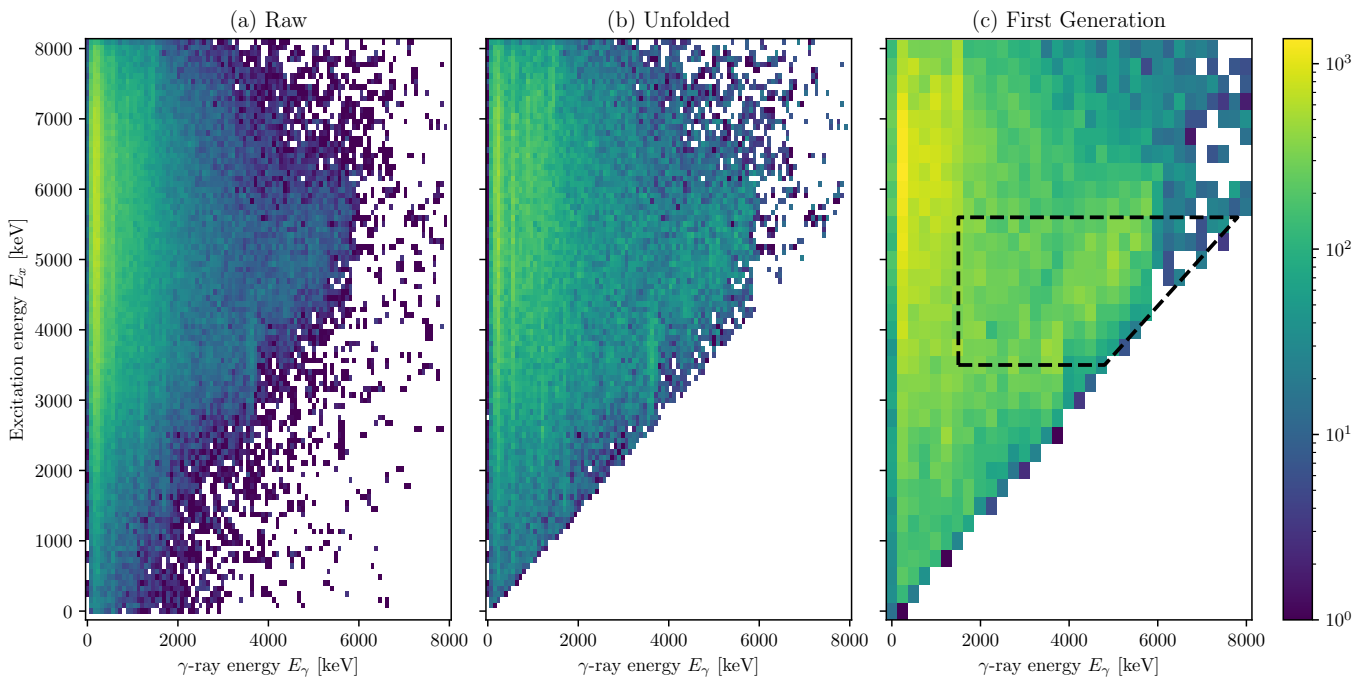


FIG. 1. Raw excitation- $\gamma$  coincidence (a), unfolded (b) and first generation (c) matrices (see text for details).

the unfolded matrix in order to deduce the distribution of primary  $\gamma$ -rays emitted from each excitation bin, resulting in the *first generation* matrix shown in Fig. 1(c).

The first generation matrix is proportional to the  $\gamma$ -ray transmission coefficients  $\mathcal{T}(E_\gamma)$  and the NLD  $\rho(E_f = E_x - E_\gamma)$  at the final excitation energy  $E_f$  [6]

$$\Gamma(E_x, E_\gamma) \propto \mathcal{T}(E_\gamma)\rho(E_f = E_x - E_\gamma). \quad (1)$$

The NLD and transmission coefficients are extracted by normalizing the first-generation  $\gamma$ -ray spectra for each excitation bin and by fitting the experimental matrix with a theoretical matrix [6]

$$\Gamma_{\text{th}}(E_x, E_\gamma) = \frac{\mathcal{T}(E_\gamma)\rho(E_x - E_\gamma)}{\sum_{E_\gamma=E_\gamma^{\text{min}}}^{E_x} \mathcal{T}(E_\gamma)\rho(E_x - E_\gamma)} \quad (2)$$

by minimizing

$$\chi^2 = \sum_{E_x, E_\gamma} \left( \frac{\Gamma(E_\gamma, E_x) - \Gamma_{\text{th}}(E_\gamma, E_x)}{\Delta\Gamma(E_\gamma, E_x)} \right)^2, \quad (3)$$

where  $\mathcal{T}(E_\gamma)$  and  $\rho(E_f = E_x - E_\gamma)$  are treated as free parameters for each  $\gamma$ -ray energy  $E_\gamma$  and final energy  $E_f$ , respectively. To ensure that only statistical transitions are considered a minimum  $\gamma$ -ray energy of 1.5 MeV was set. Similarly, only excitation energy bins between 3.5 and 5.6 MeV were included in the fit.

The resulting  $\gamma$ -ray transmission coefficients are converted to  $\gamma$ SF by

$$f(E_\gamma) = \frac{\mathcal{T}(E_\gamma)}{2\pi E_\gamma^3}$$

under the assumption that the transmission coefficients are dominated by dipole transitions.

The theoretical first generation matrix, (2), is invariant under transformation of NLD and  $\gamma$ SF [6]

$$\begin{aligned} \tilde{\rho}(E_f) &= A\rho(E_f)e^{\alpha E_f} \\ \tilde{f}(E_\gamma) &= Bf(E_\gamma)e^{\alpha E_\gamma}, \end{aligned} \quad (4)$$

where  $A$ ,  $B$  and  $\alpha$  are transformation parameters. This means that the extracted NLD and  $\gamma$ SF do not represent the physical NLD and  $\gamma$ SF, but contain information on the functional shape. To deduce the absolute values of the NLD and  $\gamma$ SF the extracted NLD and  $\gamma$ SF will have to be normalized to auxiliary data.

### III. NORMALIZATION OF NLD AND $\gamma$ SF

Many nuclei along the island of stability have auxiliary data available with which the normalization of the NLDs and  $\gamma$ SFs is achieved. Typical data used for this purpose are the level density from resolved discrete states, the level density at the neutron separation energy from s- and/or p-wave neutron resonance spacing data and the average radiative widths of s-wave neutron resonances. When applying the Oslo method, NLDs do not extend to the neutron separation energy as the method probes the NLD at the final excitation energy  $E_f = S_n - E_\gamma$ , the maximum energy possible to be considered in the first generation matrix is the neutron separation energy (depending on reaction kinematics) [30]. Hence, the measured NLDs are typically interpolated to the NLDs from resonance data at the neutron separation energy.

For nuclei where neutron resonance data are not available these have generally been estimated from systematics of nuclei in their vicinity. Neither for the case of  $^{67}\text{Ni}$  nor for surrounding nuclei are neutron resonance data available. The situation is further aggravated by an incomplete level scheme at low excitation energies resulting in an unreliable level density of resolved discrete states. With the absence of any reliable normalization points the only practical solution for normalizing the NLD and  $\gamma\text{SF}$  is the reliance on model estimates.

### A. Bayesian analysis

Despite the lack of auxiliary data for normalization there is still valuable information on the NLD and  $\gamma\text{SF}$  that can be obtained from the non-normalized experimental NLD and  $\gamma\text{SF}$ . Through the application of the simple principle that the NLD increases with excitation energy places limits on the possible values of the slope parameter ( $\alpha$  in Eq. (4)). This in turn constrains the shape of the  $\gamma\text{SF}$ , giving valuable insight into models that can reasonably reproduce the  $\gamma\text{SF}$ . This can be taken a step further, given a set of models for the NLD and  $\gamma\text{SF}$ , it can be explored what the appropriate normalization and model parameters are for the best agreement between models and experimental data. To perform such an analysis we apply Bayesian statistics. Analyzing Oslo method data within a Bayesian statistics framework has previously been demonstrated by Midtbø *et al.* in Ref. [7] and our analysis is based on the framework presented therein. The starting point of the normalization analysis is Bayes' theorem

$$P(\boldsymbol{\theta}|\{\rho_i\}, \{f_i\}) = \frac{\mathcal{L}(\{\rho_i\}, \{f_i\}|\boldsymbol{\theta})P(\boldsymbol{\theta})}{P(\{\rho_i\}, \{f_i\})}, \quad (5)$$

where  $P(\boldsymbol{\theta}|\{\rho_i\}, \{f_i\})$  is the posterior probability of a set of normalization and model parameters  $\boldsymbol{\theta} = (A, B, \alpha, \boldsymbol{\theta}_{\text{NLD}}, \boldsymbol{\theta}_{\gamma\text{SF}})$ , given a set of non-normalized NLD points  $\{\rho_i\}$  and  $\gamma\text{SF}$  points  $\{f_i\}$ . The likelihood  $\mathcal{L}(\{\rho_i\}, \{f_i\}|\boldsymbol{\theta})$  is the probability of measuring non-normalized NLD and  $\gamma\text{SF}$  given the set of parameters  $\boldsymbol{\theta}$ .  $P(\boldsymbol{\theta})$  is the prior probability of a set of normalization and model parameters. The evidence  $P(\{\rho_i\}, \{f_i\})$  is the probability of measuring the non-normalized NLD and  $\gamma\text{SF}$ . With the assumption of Gaussian distributed uncertainties of the measured non-normalized NLD and  $\gamma\text{SF}$  leads to the likelihood

$$\mathcal{L}(\boldsymbol{\theta}) = \prod_i \mathcal{L}_i(\boldsymbol{\theta}), \quad (6)$$

with

$$\ln \mathcal{L}_{\text{discrete}} = \sum_j \ln \frac{1}{\sqrt{2\pi}\sigma_{\rho_j, \text{Oslo}}(\boldsymbol{\theta})} - \frac{1}{2} \sum_j \left( \frac{\rho_{j, \text{discrete}} - \rho_{j, \text{Oslo}}(\boldsymbol{\theta})}{\sigma_{\rho_j, \text{Oslo}}(\boldsymbol{\theta})} \right)^2, \quad (7)$$

$$\ln \mathcal{L}_{\text{NLD}} = \sum_j \ln \frac{1}{\sqrt{2\pi}\sigma_{\rho_j, \text{Oslo}}(\boldsymbol{\theta})} - \frac{1}{2} \sum_j \left( \frac{\rho_{j, \text{model}}(\boldsymbol{\theta}) - \rho_{j, \text{Oslo}}(\boldsymbol{\theta})}{\sigma_{\rho_j, \text{Oslo}}(\boldsymbol{\theta})} \right)^2, \quad (8)$$

$$\ln \mathcal{L}_{\gamma\text{SF}} = \sum_j \ln \frac{1}{\sqrt{2\pi}\sigma_{f_j, \text{Oslo}}(\boldsymbol{\theta})} - \frac{1}{2} \sum_j \left( \frac{f_{j, \text{model}}(\boldsymbol{\theta}) - f_{j, \text{Oslo}}(\boldsymbol{\theta})}{\sigma_{f_j, \text{Oslo}}(\boldsymbol{\theta})} \right)^2, \quad (9)$$

$$\ln \mathcal{L}_{^{68}\text{Ni}} = -\frac{1}{2} \sum_j \left( \frac{f_{j, \text{model}}(\boldsymbol{\theta}) - f_{j, ^{68}\text{Ni}}(\boldsymbol{\theta})}{\sigma_{j, ^{68}\text{Ni}}} \right)^2. \quad (10)$$

Here,  $\mathcal{L}_{\text{discrete}}$  represents the likelihood of measuring a set of NLDs given the known level density from discrete levels  $\rho_{j, \text{discrete}}$ ,  $\mathcal{L}_{\text{NLD}}$  is the likelihood given a specific NLD model and  $\mathcal{L}_{\gamma\text{SF}}$  is the likelihood given a  $\gamma\text{SF}$ . The  $\mathcal{L}_{^{68}\text{Ni}}$  likelihood is included to further constrain the  $\gamma\text{SF}$  using the measured  $\gamma\text{SF}$  in  $^{68}\text{Ni}$  as the  $\gamma\text{SF}$  above the neutron separation energy are typically very similar in neighboring nuclei. Further discussion on models and parameter priors will follow in Sect. IIIB and Sect. IIIC, respectively.  $\rho_{j, \text{Oslo}}(\boldsymbol{\theta})$ ,  $(f_{j, \text{model}}(\boldsymbol{\theta}))$  and  $\sigma_{\rho_j, \text{Oslo}}(\boldsymbol{\theta})$  ( $\sigma_{f_j, \text{Oslo}}(\boldsymbol{\theta})$ ) are the normalized NLD ( $\gamma\text{SF}$ ) and standard deviation, given a set of normalization parameters  $A, B, \alpha \in \boldsymbol{\theta}$ , respectively (see Eq. 4).

Instead of NLDs from resolved discrete states we have considered level densities based on the counting of levels from large-scale shell model (SM) calculations of ref. [31]. For shell model results utilizing the `ca48mh1g` interaction, see Refs.[10, 31] for details. Justification for this choice is based on the comparison between known low-lying levels and shell model results of other Ni isotopes [10]. These are shown to reproduce experimental NLDs with reasonable accuracy, see .

To perform the actual Bayesian analysis, model and normalization parameters were sampled using the Bayesian nested sampling algorithm `MultNest` [32–34] in the `PyMultinest` package [35]. Final, model-dependent, normalized NLD and  $\gamma\text{SF}$  are obtained by averaging the posterior for each combination of NLD and  $\gamma\text{SF}$  model.

### B. Models

A total of three NLD models and four  $\gamma\text{SF}$  models have been considered, making the total number of inferred posteriors twelve. In this section we will describe

the models considered.

### NLD

For energies above the point where the model space of the shell model calculation is exhausted the NLD has been modeled with three different models. These include the BSFG model [36, 37]

$$\rho_{\text{BSFG}}(E_x) = \frac{\sqrt{\pi} \exp(2\sqrt{a(E_x - \delta)})}{12\sigma a^{1/4}(E_x - \delta)^{5/4}}, \quad (11)$$

where  $a$  is the level density parameter,  $\delta$  is the energy shift and  $\sigma$  is the spin-cutoff parameter. The CT model [38]

$$\rho_{\text{CT}}(E_x) = \frac{1}{T} e^{\frac{E_x - \delta}{T}}, \quad (12)$$

where  $T$  is the nuclear temperature and  $\delta$  is an energy shift parameter. Lastly, tabulated Hartree-Fock-Bogoliubov (HFB) calculations [39] were also considered, and allowed to be re-normalized through

$$\rho_{\text{HFB}}(E_x) = \hat{\rho}_{\text{HFB}}(E_x - \delta) e^{c\sqrt{E_x - \delta}}, \quad (13)$$

where again  $\delta$  is used to denote an energy shift,  $c$  is a slope parameter and  $\hat{\rho}_{\text{HFB}}$  are the tabulated NLDs. It should be noted that  $\delta$  in eqs. (11), (12), and (13) are not the same parameters and will be sub-scripted whenever there is ambiguity which parameter is being referenced. The spin distribution for the BSFG and CT models was given by the Ericson distribution [36, 38]

$$g(E_x, J) = \exp\left(-\frac{J^2}{2\sigma^2(E_x)}\right) - \exp\left(-\frac{(J+1)^2}{2\sigma^2(E_x)}\right), \quad (14)$$

with the spin-cutoff parameterized by [40, 41]

$$\sigma^2(E_x) = \begin{cases} \sigma_d^2 & E < E_d \\ \sigma_d^2 + \frac{E - E_d}{S_n - E_d} (\sigma^2(S_n) - \sigma_d^2) & E \geq E_d, \end{cases} \quad (15)$$

where the spin distribution is constant at energies less than  $E_d = 2.0$  MeV.

### $\gamma$ SF

For the  $\gamma$ SF we have considered the Simplified version of the Modified Lorentzian model (SMLO) [42] and the microscopic Gogny-HFB plus quasi-particle random phase approximation (Gogny-HFB+QRPA) with phenomenological corrections [43]. The SMLO model describes the  $\gamma$ SF with the giant dipole resonance (GDR) for downward strength is given by

$$f_{\text{GDR}}(E_\gamma) = \frac{1}{3\pi^2 \hbar^2 c^2} \frac{\sigma_{\text{TRK}}}{1 - \exp(-E_\gamma/T)} \times \frac{2}{\pi} \frac{E_\gamma \Gamma(E_\gamma, T)}{(E_\gamma^2 - E_{\text{GDR}}^2)^2 + E_\gamma^2 \Gamma^2(E_\gamma, T)}, \quad (16)$$

where  $E_{\text{GDR}}$  is the centroid of the GDR,  $\sigma_{\text{TRK}} = 60 \frac{NZ}{A}$  is the Thomas-Reiche-Kuhn sum rule [42] and  $T$  is the temperature at the final excitation energy. The width,

$$\Gamma(E_\gamma, T) = \frac{\Gamma_{\text{GDR}}}{E_{\text{GDR}}} \left( E_\gamma + \frac{(2\pi T)^2}{E_{\text{GDR}}} \right), \quad (17)$$

depends on the final temperature and the  $\Gamma_{\text{GDR}}$  which is the width found in the upward strength function. Within the SMLO model the M1 strength is parameterized as two standard Lorentzians (SLO)

$$f_{\text{SLO}}(E_\gamma) = \frac{1}{3\pi^2 \hbar^2 c^2} \frac{E_\gamma \Gamma^2}{(E_\gamma^2 - E_r^2)^2 + (E_\gamma \Gamma)^2} \quad (18)$$

for the scissors and the spin-flip resonances. The low-energy upbend is modeled as a simple exponential [39]. From the shape of the non-normalized  $\gamma$ SF there are no obvious signs of a scissors resonance which is consistent with the relatively low estimated axial deformation of  $\beta_2 = 0.05$  [44] and has been omitted from further consideration in the model for the  $\gamma$ SF. The assumed M1 strength contributions are thus

$$f_{\text{M1}}(E_\gamma) = f_{\text{SLO}}(E_\gamma, E_{\text{sf}}, \Gamma_{\text{sf}}, \sigma_{\text{sf}}) + C \exp(-\eta E_\gamma), \quad (19)$$

where  $E_{\text{sf}}$  is the mean energy,  $\Gamma_{\text{sf}}$  is the width and  $\sigma_{\text{sf}}$  the cross-section of the spin-flip resonance. The slope of the upbend is  $\eta$ ,  $C$  the zero-limit and the assumption of M1 strength is based on results from shell model calculations [45–48].

In the second model, the Gogny-HFB+QRPA model, the downward E1 strength is given by

$$f_{\text{E1}}(E_\gamma) = c_{\text{E1}} f_{\text{E1}}^{\text{QRPA}}(E_\gamma - \delta_{\text{E1}}) + \frac{f_0 U}{1 + \exp(E_\gamma - \epsilon_0)}, \quad (20)$$

where  $f_{\text{E1}}^{\text{QRPA}}(E_\gamma)$  is the strength found in Gogny-HFB+QRPA calculations. The phenomenological parameters  $f_0$ ,  $\epsilon_0$  are free parameters and  $U$  is the excitation energy of the initial level. The strength are allowed to be scaled and shifted through the parameters  $c_{\text{E1}}$  and  $\delta_{\text{E1}}$ , respectively. The M1 strength was estimated within the SMLO model (eq. (19)).

Data points from a Coulomb dissociation measurement of  $^{68}\text{Ni}$  are also considered [49]. This features a strong narrow Pygmy dipole resonance at  $E_x \approx 9.5$  MeV which has been accounted for by including a SLO in the E1 strength. Since the extracted  $\gamma$ SF in  $^{67}\text{Ni}$  only extends to 5.8 MeV we cannot determine if such a PDR also exists in  $^{67}\text{Ni}$ . In order to account for either possibility, we have repeated the analysis both with and without the PDR. In the latter case the two lowest points of  $^{68}\text{Ni}$  were excluded in the likelihood (Eq. (10)).

### C. Parameter priors

A list of all model combinations and their parameters are listed in Table I.

TABLE I. List of all NLD and  $\gamma$ SF models considered and their parameters.

Model	$\theta_{\text{NLD}}$	$\theta_{\gamma\text{SF}}$
CT+SMLO	$T, \delta_{\text{CT}}, \sigma_d, \sigma(S_n)$	$E_{\text{GDR}}, \Gamma_{\text{GDR}}, \sigma_{\text{GDR}}, E_{\text{sf}}, \Gamma_{\text{sf}}, \sigma_{\text{sf}}, C, \eta$
CT+SMLO+PDR	$T, \delta_{\text{CT}}, \sigma_d, \sigma(S_n)$	$E_{\text{GDR}}, \Gamma_{\text{GDR}}, \sigma_{\text{GDR}}, E_{\text{PDR}}, \Gamma_{\text{PDR}}, \sigma_{\text{PDR}}, E_{\text{sf}}, \Gamma_{\text{sf}}, \sigma_{\text{sf}}, C, \eta$
CT+HFB-QRPA	$T, \delta_{\text{CT}}, \sigma_d, \sigma(S_n)$	$c_{\text{E1}}, \delta_{\text{E1}}, f_0, \epsilon_0, E_{\text{sf}}, \Gamma_{\text{sf}}, \sigma_{\text{sf}}, C, \eta$
CT+HFB-QRPA+PDR	$T, \delta_{\text{CT}}, \sigma_d, \sigma(S_n)$	$c_{\text{E1}}, \delta_{\text{E1}}, f_0, \epsilon_0, E_{\text{PDR}}, \Gamma_{\text{PDR}}, \sigma_{\text{PDR}}, E_{\text{sf}}, \Gamma_{\text{sf}}, \sigma_{\text{sf}}, C, \eta$
BSFG+SMLO	$a, \delta_{\text{BSFG}}, \sigma_d, \sigma(S_n)$	$E_{\text{GDR}}, \Gamma_{\text{GDR}}, \sigma_{\text{GDR}}, E_{\text{sf}}, \Gamma_{\text{sf}}, \sigma_{\text{sf}}, C, \eta$
BSFG+SMLO+PDR	$a, \delta_{\text{BSFG}}, \sigma_d, \sigma(S_n)$	$E_{\text{GDR}}, \Gamma_{\text{GDR}}, \sigma_{\text{GDR}}, E_{\text{PDR}}, \Gamma_{\text{PDR}}, \sigma_{\text{PDR}}, E_{\text{sf}}, \Gamma_{\text{sf}}, \sigma_{\text{sf}}, C, \eta$
BSFG+HFB-QRPA	$a, \delta_{\text{BSFG}}, \sigma_d, \sigma(S_n)$	$c_{\text{E1}}, \delta_{\text{E1}}, f_0, \epsilon_0, E_{\text{sf}}, \Gamma_{\text{sf}}, \sigma_{\text{sf}}, C, \eta$
BSFG+HFB-QRPA+PDR	$a, \delta_{\text{BSFG}}, \sigma_d, \sigma(S_n)$	$c_{\text{E1}}, \delta_{\text{E1}}, f_0, \epsilon_0, E_{\text{PDR}}, \Gamma_{\text{PDR}}, \sigma_{\text{PDR}}, E_{\text{sf}}, \Gamma_{\text{sf}}, \sigma_{\text{sf}}, C, \eta$
HFB+SMLO	$c_{\text{HFB}}, \delta_{\text{HFB}}$	$E_{\text{GDR}}, \Gamma_{\text{GDR}}, \sigma_{\text{GDR}}, E_{\text{sf}}, \Gamma_{\text{sf}}, \sigma_{\text{sf}}, C, \eta$
HFB+SMLO+PDR	$c_{\text{HFB}}, \delta_{\text{HFB}}$	$E_{\text{GDR}}, \Gamma_{\text{GDR}}, \sigma_{\text{GDR}}, E_{\text{PDR}}, \Gamma_{\text{PDR}}, \sigma_{\text{PDR}}, E_{\text{sf}}, \Gamma_{\text{sf}}, \sigma_{\text{sf}}, C, \eta$
HFB+HFB-QRPA	$c_{\text{HFB}}, \delta_{\text{HFB}}$	$c_{\text{E1}}, \delta_{\text{E1}}, f_0, \epsilon_0, E_{\text{sf}}, \Gamma_{\text{sf}}, \sigma_{\text{sf}}, C, \eta$
HFB+SMLO+PDR	$c_{\text{HFB}}, \delta_{\text{HFB}}$	$c_{\text{E1}}, \delta_{\text{E1}}, f_0, \epsilon_0, E_{\text{PDR}}, \Gamma_{\text{PDR}}, \sigma_{\text{PDR}}, E_{\text{sf}}, \Gamma_{\text{sf}}, \sigma_{\text{sf}}, C, \eta$

To select the priors for the normalization parameters  $A$ ,  $B$  and  $\alpha$ , an approximate solution was first found by calculating the maximum-likelihood estimator (MLE)  $\hat{\theta}$  by minimizing the likelihood (Eq. (6)). Both  $A$  and  $B$  are assumed to have a Gaussian prior distribution truncated at zero (negative values are nonphysical) with the mean  $\mu$  given by MLE with width  $\sigma = 10\mu$ . The slope parameter  $\alpha$  has a Gaussian prior distribution with mean  $\mu$  again given by MLE but with a width of  $1 \sigma = 1 \text{ MeV}^{-1}$ .

For the model parameters the priors were represented as either Gaussians or truncated Gaussians for the physical or nonphysical values, respectively. For the NLD models fairly weak informed priors were used. In the case of the BSFG model the level density parameter  $a$  mean value of  $\mu = 8.2 \text{ MeV}$  was selected as the approximate mean of the systematics from Refs. [37, 50], Refs. [51, 52] and Ref. [52] with width  $\sigma = \mu$ . The shift parameter  $\delta_{\text{BSFG}}$  is a Gaussian with  $\mu = 0 \text{ MeV}$  and  $\sigma = 10 \text{ MeV}$ . Similarly the CT model priors were selected from the systematics of Ref. [52] with widths of  $\sigma = 2 \text{ MeV}$  for the temperature and  $\sigma = 10 \text{ MeV}$  for the shift parameter  $\delta_{\text{CT}}$ . The slope and shift parameters  $c$  and  $\delta_{\text{HFB}}$  for the HFB was centered around  $0 \text{ MeV}^{-1/2}$  and  $0 \text{ MeV}$ , respectively with a width of  $1 \text{ MeV}^{-1/2}$  and  $1 \text{ MeV}$ , respectively. The discrete spin-cutoff parameter  $\sigma_d = 2.50(25)$  was found by examining the tabulated shell model levels while the spin-cutoff at the neutron separation energy is  $\sigma(S_n) = 3.80(38)$  from an average of spin-cut off models in [37, 39, 51]. In both cases an uncertainty of 10% was assumed. The priors for all NLD model parameters are listed in Table II.

The parameters for the SMLO model were taken from the systematics in [42]. Unless an uncertainty was provided it was assumed to be 10%. The scale  $c_{\text{E1}}$  and shift  $\delta_{\text{E1}}$  for the Gogny-HFB+QRPA was assumed to be centered around 1 and 0 MeV, respectively, with a width of 0.5 MeV for both. The phenomenological parameters  $f_0$  and  $\epsilon_0$  are taken from [43]. The spin-flip and upbend parameters were taken from [42] assuming 10% uncertainty, except for  $C$ , where the width was assumed to be the same as the mean. Lastly, the PDR parameters were taken from [49]. All priors parameters related to the  $\gamma$ SF models are listed in Table III.

TABLE II. Gaussian model parameter priors used for the extrapolation of the NLD between the experimental points and the neutron separation energy.

Parameter	$\mu$	$\sigma$
$a$	8.2 MeV	8.2 MeV
$\delta$ (BSFG)	0 MeV	10 MeV
$T$	0.958 MeV	2 MeV
$\delta$ (CT)	-0.359 MeV	10 MeV
$c$ (HFB)	$0 \text{ MeV}^{-1/2}$	$1 \text{ MeV}^{-1/2}$
$\delta$ (HFB)	0 MeV	1 MeV
$\sigma_d$	2.5	0.25
$\sigma(S_n)$	3.8	0.38

TABLE III. Model parameter priors used for the  $\gamma$ SF models extrapolated to the extracted  $\gamma$ SF of  $^{67}\text{Ni}$ .

Parameter	$\mu$	$\sigma$
$E_{\text{GDR}}$	17.68 MeV	0.19 MeV
$\Gamma_{\text{GDR}}$	6.0 MeV	2.8 MeV
$\sigma_{\text{GDR}}$	978 mb MeV	98 mb MeV
$c_{\text{E1}}$	1	0.5
$\delta_{\text{E1}}$	0 MeV	0.5 MeV
$f_0$	$2.5 \times 10^{-10} \text{ MeV}^{-4}$	$2.5 \times 10^{-10} \text{ MeV}^{-4}$
$\epsilon_0$	4 MeV	1 MeV
$E_{\text{PDR}}$	9.55 MeV	0.17 MeV
$\Gamma_{\text{PDR}}$	1.02	0.26 MeV
$\sigma_{\text{PDR}}$	27.4 mb	5.6 mb
$E_{\text{sf}}$	8.93 MeV	0.90 MeV
$\Gamma_{\text{sf}}$	4.0 MeV	0.4 MeV
$\sigma_{\text{sf}}$	1.0 mb	0.1 mb
$C$	$3.5 \times 10^{-8} \text{ MeV}^{-3}$	$3.5 \times 10^{-8} \text{ MeV}^{-3}$
$\eta$	0.8 1/MeV	0.08 1/MeV

## D. Results

The resulting normalized NLD and  $\gamma$ SF are shown in Figs. 2 and 3. Neither the inclusion nor exclusion of the PDR has a noticeable effect on the normalized NLD, while the effect was minimal on the  $\gamma$ SF, see Fig. 4. The NLD and  $\gamma$ SF is therefore averaged over all model combinations.

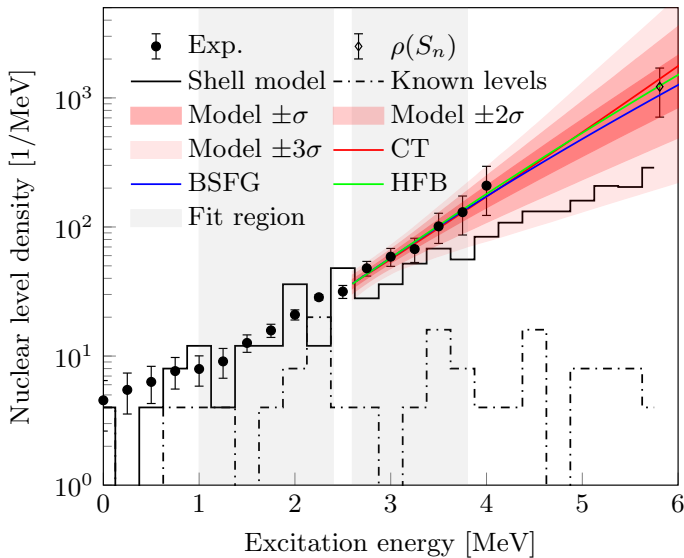


FIG. 2. The measured nuclear level density of  $^{67}\text{Ni}$  is shown by the black circles while the black line shows the NLD from large scale SM calculations of [31]. The black dash-dotted line shows the NLD from known discrete levels [53, 54]. The red, blue and green lines show the average for the CT, BSFG and HFB models, respectively. The red shaded area indicates the  $\pm 1\sigma$ ,  $\pm 2\sigma$  and  $\pm 3\sigma$  credibility intervals. The black triangle shows the NLD at the neutron separation energy.

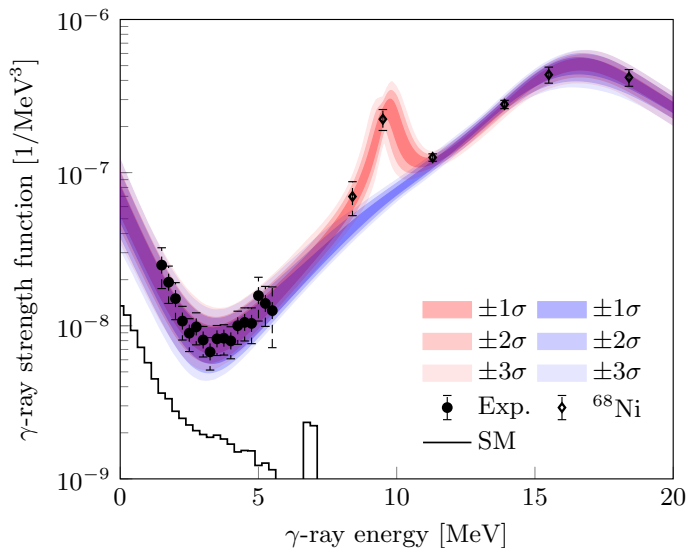


FIG. 3. The measured  $\gamma$ -ray strength function of  $^{67}\text{Ni}$  is shown by the black circles while the black line shows the M1-strength found in large scale SM calculations from [31]. The red and blue shaded area indicates the  $\pm 1\sigma$ ,  $\pm 2\sigma$  and  $\pm 3\sigma$  credibility intervals for the models including the PDR and the models excluding the PDR, respectively. The black diamonds are the  $\gamma$ SF data of  $^{68}\text{Ni}$  measured by Rossi *et al.* [49].

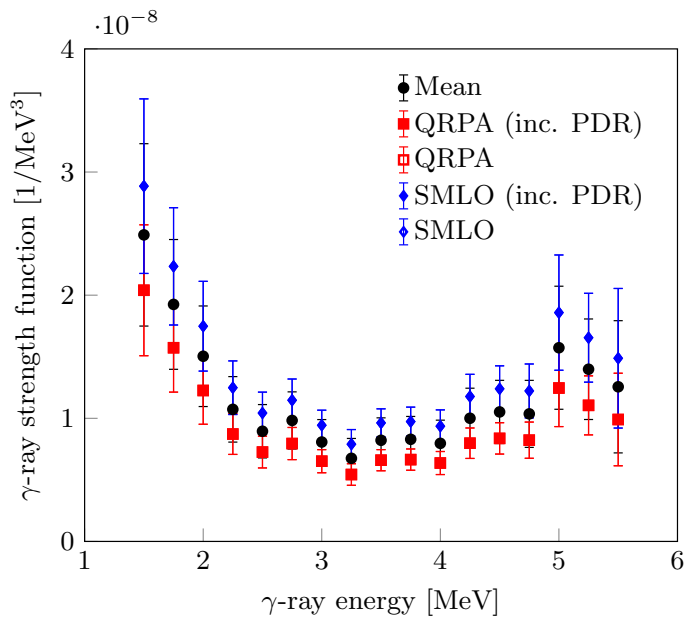


FIG. 4. Comparison of the various  $\gamma$ SF normalizations including and excluding the PDR. The black circles shows the average normalized  $\gamma$ SF.

#### IV. HAUSER-FESHBACH CALCULATIONS

The measured NLD and  $\gamma$ SF in  $^{67}\text{Ni}$  were used in Hauser-Feshbach calculations to constrain the neutron capture cross section of  $^{66}\text{Ni}$ . From each posterior sample of normalization and model parameters tabulated NLD and  $\gamma$ SF values were generated from linear interpolation and used as input to the TALYS<sup>1</sup> reaction code [55]. Since the level scheme of  $^{67}\text{Ni}$  is far from complete only the first two discrete levels were used in the Hauser-Feshbach calculations, while above those the measured NLD was used.

In Fig. 5, the average of all calculated capture cross sections, based on the experimental data, is shown together with the TALYS default input and calculations with all combinations of NLD and  $\gamma$ SF models as implemented in TALYS. Fig. 5 also includes results from the TENDL [56], and JEFF-3.3 [57] evaluations.

#### V. DISCUSSION

The Oslo method relies on external nuclear data for the normalization. In the absence of those, additional uncertainties may be induced and model dependencies may become significant. This is apparent through the relatively large uncertainties toward  $S_n$  on the measured NLD for  $^{67}\text{Ni}$ .

The challenge specific to inverse kinematic reactions is the Lorentz boost which causes a strong angular de-

<sup>1</sup> Version 1.96

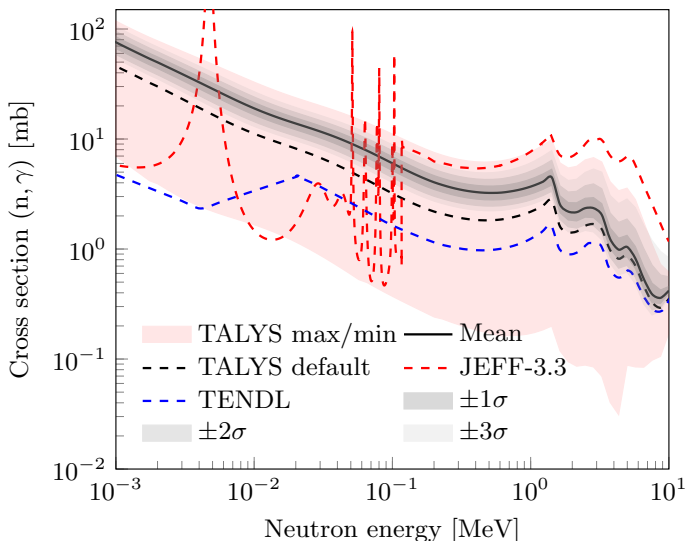


FIG. 5. The mean calculated capture cross section from the sampled NLD and  $\gamma$ SF are given by the black line. The gray shaded area shows the  $\pm 1\sigma$ ,  $\pm 2\sigma$  and  $\pm 3\sigma$  credibility intervals. The black dashed line are the capture cross section with TALYS default values. The red shaded area shows the upper and lower limit based on all NLD and  $\gamma$ SF models available in TALYS. The red and blue dashed lines shows the JEFF-3.3 library [57] and the TENDL library [56], respectively.

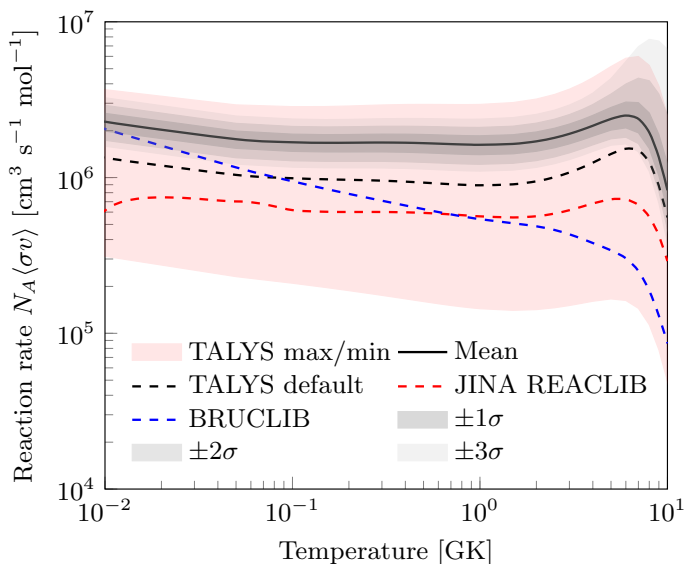


FIG. 6. The mean calculated capture rate from the sampled NLD and  $\gamma$ SF are given by the black line. The gray filled area shows the  $\pm 1\sigma$ ,  $\pm 2\sigma$  and  $\pm 3\sigma$  credibility intervals. The black dashed line are the capture rate with TALYS default. The red and blue dashed lines are the reaction rates from JINA REACLIB v1.1 [58] and BRUCLIB [59], respectively. The red shaded area shows the upper and lower limit based on the NLD and  $\gamma$ SF models included in the uncertainty estimation of Ref. [15].

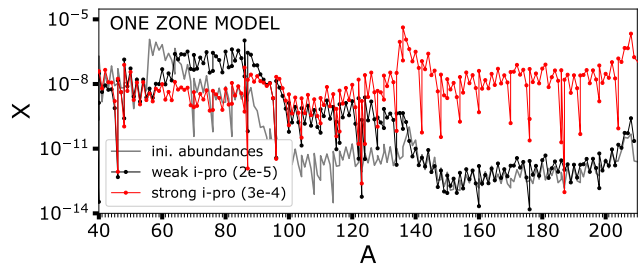


FIG. 7. Final nuclei mass fractions (after decays) as a function of mass number after a weak (black) and a strong (red)  $i$ -process using the one-zone model. The initial proton mass fraction is indicated in parenthesis (see text for details). The grey pattern shows the initial abundances.

pendence in the kinematic reconstruction of the residual excitation energy. This leads to an excitation-energy resolution which is limited by the angular opening of the particle telescope's active areas. The consequences are most apparent in the NLD where very little structures are visible.

In contrast, the measured  $\gamma$ SF still retains noticeable features and clearly exhibits a well established enhancement for  $E_x < 4$  MeV similar to those found in other Ni isotopes [10, 60–64]. Its observation indicates that the upbend is a structure which exists also away from stability. The upbend in  $^{67}\text{Ni}$  is predicted to be due to M1 strength, based on large-scale shell model calculations [31], and shown by the black solid line in Fig. 3. The significant strength in the enhancement and the simultaneous absence of a measurable scissors resonance may be supportive of the suggested connection of the two structures [46, 65], although results on the  $\gamma$ SF in  $^{142,144-151}\text{Nd}$  seem to contradict this [66].

The calculated  $^{66}\text{Ni}(n, \gamma)$  capture cross section in Fig. 5 features an uncertainty of  $\approx 40\%$ , constraining the cross section considerably. It is interesting to note that our cross section, lies consistently higher than the recommended values as provided in TALYS, JENDEL-5, and TENDL but is smaller than the JEFF 3.3 for  $E_n > 100$  keV. These differences highlight the necessity for measurements of NLDs and  $\gamma$ SFs, especially for nuclei away from stability.

In Ref. [15] the capture rate was allowed to vary within a factor of 10 and is significantly constrained by our results, as shown in Fig. 6. Our results shows that the reaction rate is rather high compared with the rate used in Ref. [15]. This suggests a short exposure time for the weak  $i$ -process, and could help pinpoint details in the stellar environment responsible for the production of neutrons.



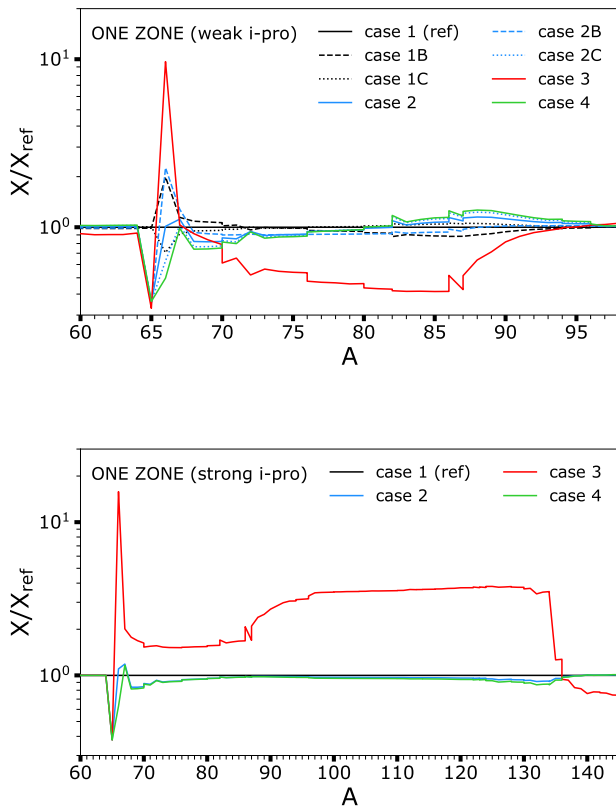


FIG. 8. Final nuclei mass fractions (after decays) as a function of mass number after a weak (top panel) and a strong (bottom) i-process using the one-zone model. The abundances are normalized by the abundances of the case 1. The 8 cases correspond to the 8 different combinations of rates indicated in Table IV (cases 1B, 1C, 2B and 2C are not shown in the bottom panel for clarity).

## VI. ASTROPHYSICAL IMPLICATIONS

The  $^{66}\text{Ni}(n, \gamma)$  capture rate was suggested to be of key importance for the overall production of heavy elements during the i-process nucleosynthesis taking place in Sakurai’s object or rapidly accreting white dwarfs [15]. One possible astrophysical site with similar i-process conditions are low-metallicity low-mass stars during the early thermally pulsating Asymptotic Giant Branch (AGB) phase [67–71]. During this stage, protons can be engulfed by the convective thermal pulse. As they are transported downwards by convection in a timescale of about 1 hr, they are burnt rapidly by  $^{12}\text{C}(p, \gamma)^{13}\text{N}$ . After the decay of  $^{13}\text{N}$  to  $^{13}\text{C}$  in about 10 min, the reaction  $^{13}\text{C}(\alpha, n)$  is activated at the bottom of the thermal pulse and leads to neutron densities of up to  $\sim 10^{15} \text{ cm}^{-3}$ . Stellar modeling was performed with the stellar evolution code STAREVOL [72–74]. A  $1 M_{\odot}$  AGB model at a metallicity of  $[\text{Fe}/\text{H}] = -2.5$  is considered. This model is discussed in detail in Ref. [71].

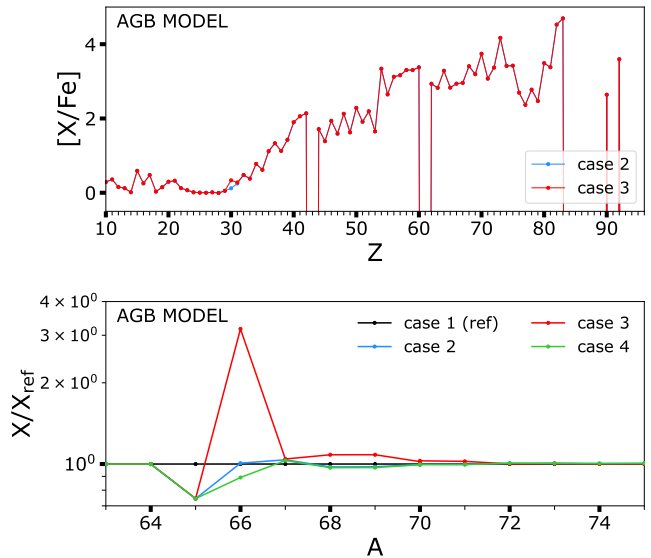


FIG. 9. Final surface abundances (after decays) for a full AGB stellar model. Top:  $[\text{X}/\text{Fe}]$  ratios, defined as  $[\text{X}/\text{Fe}] = \log_{10}(N_{\text{X}}/N_{\text{Fe}})_{\star} - \log_{10}(N_{\text{X}}/N_{\text{Fe}})_{\odot}$  with  $N_{\text{X}}$  the number density of an element X. The first and second  $\log_{10}$  terms refer to the abundances of the model and the Sun, respectively. Bottom: same as Fig. 8. The 4 cases correspond to the 4 different combinations of rates indicated in Table IV.

We estimated the impact of the new  $^{66}\text{Ni}(n, \gamma)$  rate on the i-process nucleosynthesis in these objects. The effects are evaluated on both multi-zone stellar evolution models and in one-zone nucleosynthesis calculations. We used a reaction network including 1160 nuclei, linked through 2123 nuclear reactions ( $n$ -,  $p$ -,  $\alpha$ -captures and  $\alpha$ -decays) and weak interactions (electron captures,  $\beta$ -decays). Nuclear reaction rates were taken from BRUSLIB, the Nuclear Astrophysics Library of the Université Libre de Bruxelles<sup>2</sup> [59] and the updated experimental and theoretical rates from the NETGEN interface [75]. Additional details can be found in Refs. [71, 76, 77]. In our sensitivity analysis, eight cases were investigated. We consider, for the  $^{66}\text{Ni}(n, \gamma)$  reaction, the recommended Maxwellian-averaged cross section (MACS) from this work ( $10.7 \pm 5 \text{ mb}$  at 30 keV) as well as the minimum (1 mb at 30 keV) and maximum (19 mb at 30 keV) rates predicted by a global unconstrained TALYS calculation. Additionally, the rate of  $^{65}\text{Ni}(n, \gamma)$  was also varied because  $^{65}\text{Ni}$  has a half-life of  $\sim 2.5 \text{ hr}$  (55 hr for  $^{66}\text{Ni}$ ), which is fast enough to partially bypass the neutron capture during the i-process. For  $^{65}\text{Ni}(n, \gamma)$ , we considered the minimum (10 mb at 30 keV) and maximum (70 mb at 30 keV) MACS predicted by TALYS for different NLD and  $\gamma$ SF models. We also considered the uncertainties related to the nominal  $^{66}\text{Ni}(n, \gamma)$  MACS evaluated in this

<sup>2</sup> Available at <http://www.astro.ulb.ac.be/bruslib/>

TABLE IV. The different cases considered for the rates of  $^{65}\text{Ni}(n, \gamma)$  and  $^{66}\text{Ni}(n, \gamma)$  for the one-zone and stellar model calculations.

	$^{65}\text{Ni}(n, \gamma)$	$^{66}\text{Ni}(n, \gamma)$
case 1	TALYS min	nominal
case 1B	TALYS min	nominal $- 5$ mb
case 1C	TALYS min	nominal $+ 5$ mb
case 2	TALYS max	nominal
case 2B	TALYS max	nominal $- 5$ mb
case 2C	TALYS max	nominal $+ 5$ mb
case 3	TALYS max	TALYS min
case 4	TALYS max	TALYS max

study by varying it by  $\pm 5$  mb at 30 keV (cases 1B, 1C, 2B and 2C). The different cases considered are reported in Table IV.

The initial abundances of the one-zone model correspond to the chemical composition in the thermal pulse of the AGB stellar model, just before the start of the proton ingestion event. The temperature and density were fixed to 220 MK and  $2500 \text{ g cm}^{-3}$ , respectively, which are typical values in the pulse of low-metallicity AGB models. The nucleosynthesis was calculated over a total time of  $2 \times 10^5 \text{ s}$  ( $\sim 2.3$  days). To mimic the proton ingestion episode in the one-zone model, an initial abundance of protons was set to  $2 \times 10^{-5}$  and  $3 \times 10^{-4}$  leading to maximum neutron densities of  $N_{n, \text{max}} = 1.5 \times 10^{14} \text{ cm}^{-3}$  and  $6.7 \times 10^{14} \text{ cm}^{-3}$ , respectively. For a low initial proton abundance, a weak i-process develops and elements up to the first peak ( $A \lesssim 90$ ) are synthesized (Fig. 7, black pattern). With more protons, a larger neutron density is reached and elements of the third peak (Fig. 7, red pattern) are produced. For this particular case, the final chemical composition is found to be very similar to that of the full multi-zone AGB model where densities up to  $N_n = 2.1 \times 10^{15} \text{ cm}^{-3}$  are reached.

As shown in Fig. 8, increasing the rate of  $^{65}\text{Ni}(n, \gamma)$  (case 2) leads to a smaller production of  $^{65}\text{Cu}$  (as a result of  $^{65}\text{Ni}$  decay) by a factor of  $\sim 3$  in both weak and strong i-process cases. Lowering  $^{66}\text{Ni}(n, \gamma)$  (case 3) has the strongest impact since  $^{66}\text{Ni}$  now acts as a bottleneck. In the weak i-process case (Fig. 8, top panel), it leads to an overproduction of  $^{66}\text{Zn}$  by a factor of  $\sim 10$  to the detriment of  $70 < A < 90$  isotopes ( $30 < Z < 40$ ), which are underproduced by a factor of  $\sim 3$  at maximum. For a higher neutron density (Fig. 8, bottom panel), the production of  $66 < A < 135$  isotopes ( $28 < Z < 54$ ) is enhanced by a factor of typically 2 – 4. The uncertainties on the nominal  $^{66}\text{Ni}(n, \gamma)$  MACS obtained in this work ( $\pm 5$  mb at 30 keV) induce a variation of about a factor of 3 at  $A = 66$  (dashed lines in Fig. 8, top panel).

Ref. [15] investigated the case of a weak i-process using one-zone models with an initial metallicity of  $[\text{Fe}/\text{H}] = -1.6$  ( $[\text{Fe}/\text{H}] = -2.5$  here) and different reaction rates (most of  $(n, \gamma)$  rates coming from the JINA REACLIB library [58]). Although the physical inputs are different, in the case of a weak i-process the results are qualitatively

similar to those of Ref. [15]: an underproduction of the elements with  $32 < Z < 42$  when adopting a low  $^{66}\text{Ni}(n, \gamma)$  rate.

However, when considering a full multi-zone AGB calculation, the impact of  $^{66}\text{Ni}(n, \gamma)$  is strongly damped (Fig. 9). The overproduction of  $^{66}\text{Zn}$  in case 3 is clearly present but the enrichment is a factor of  $\sim 3$  lower. In the stellar model, multiple zones with different temperatures, densities, chemical compositions and irradiations are mixed together by convection leading to a dilute production of the elements, an effect that cannot be captured by one-zone calculations.

The impact of the  $^{66}\text{Ni}(n, \gamma)$  reaction appears to be marginal in low-metallicity AGB stars experiencing i-process nucleosynthesis. It shows that one-zone calculations should be taken with caution. We should also emphasize that only one i-process site was investigated and we cannot exclude a different impact of  $^{66}\text{Ni}(n, \gamma)$  in other sites such as e.g. rapidly accreting white dwarfs [78].

## VII. SUMMARY

In this paper we have presented experimental NLD and  $\gamma\text{SF}$  of the unstable  $^{67}\text{Ni}$  nucleus. It is the first time the Oslo method has been applied to an inverse kinematics experiment with a radioactive beam. Due to the lack of reliable nuclear data for  $^{67}\text{Ni}$  the NLD and  $\gamma\text{SF}$  are normalized to model predictions resulting in large uncertainties. Hauser-Feshbach calculations were performed with the extracted NLD and  $\gamma\text{SF}$  to find the neutron capture cross section of  $^{66}\text{Ni}$ . The result of these calculations showed a rather high capture rate compared to the theoretical range, and can help improve our understanding of the i-process nucleosynthesis. In agreement with Ref. [15], we find that the reaction  $^{66}\text{Ni}(n, \gamma)$  acts as bottleneck when using one-zone models. Nevertheless, the impact is strongly damped in multi-zone low-metallicity AGB stellar models experiencing i-process nucleosynthesis. This reaction may however have a different impact in other i-process sites.

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### **Appendix: Shell model level density in Ni isotopes**

Fig. 10 and 11 compares the experimental NLD of  $^{60,64}\text{Ni}$  [60, 61] and  $^{59,63,65,69}\text{Ni}$  [60, 62–64], respectively, with the NLD found in large-scale SM calculations of [31].

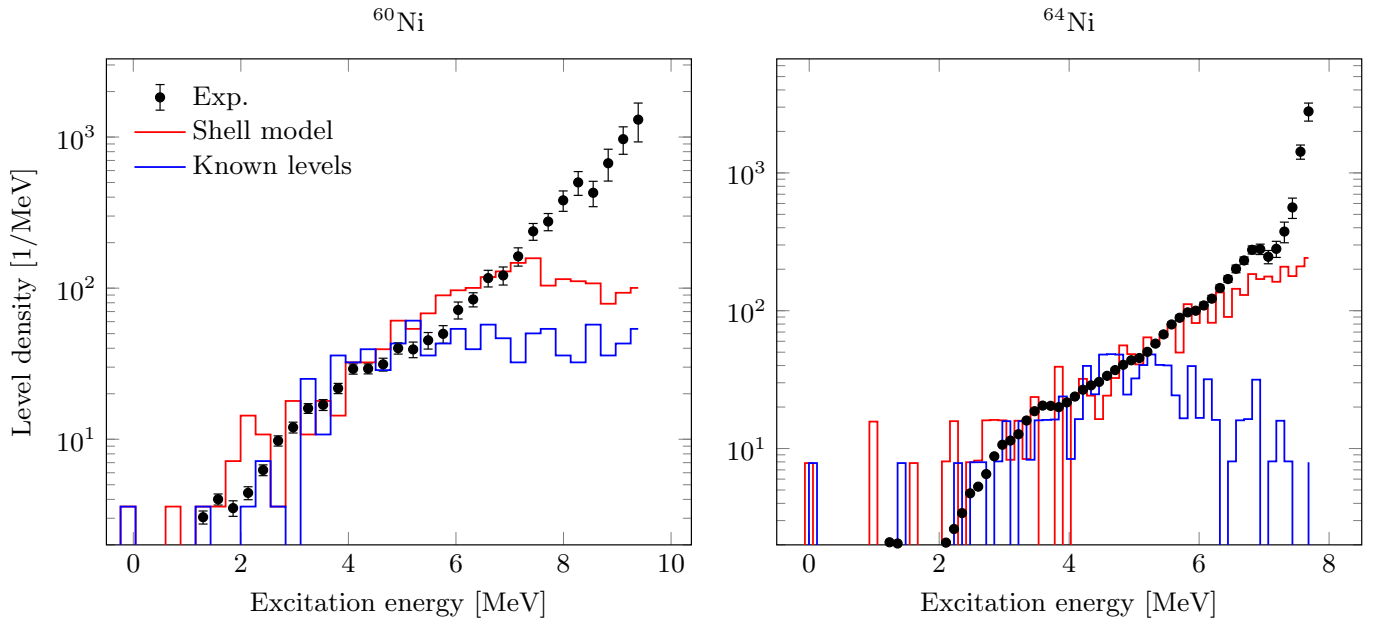


FIG. 10. Measured NLD of even-A Ni nuclei [60, 61] compared with SM calculations from [31].

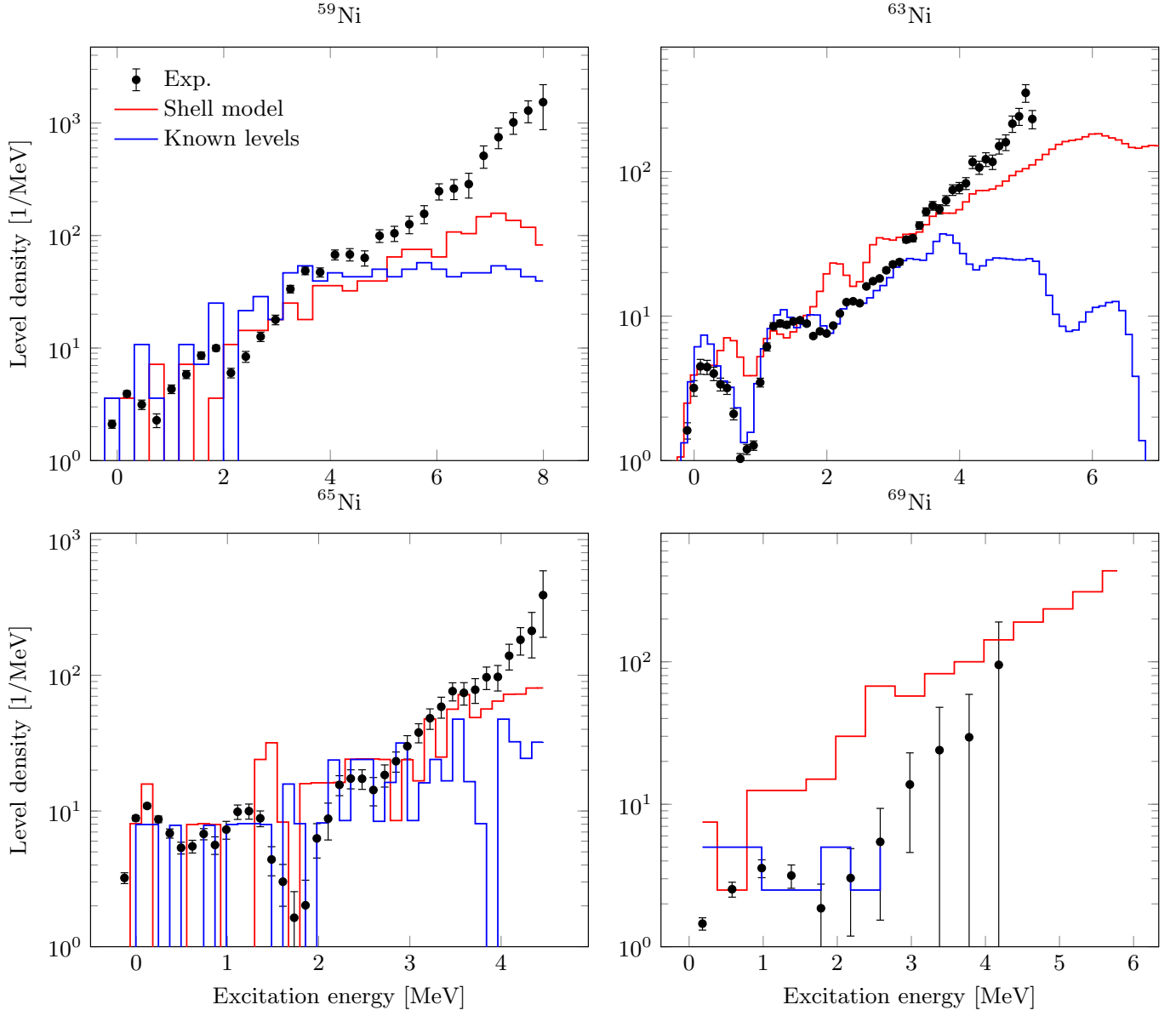


FIG. 11. Measured NLD of odd-A Ni nuclei [60, 62–64] compared with SM calculations with from [31].

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