# In-band Full-duplex Radar-communication System

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Abstract—In-band full-duplex (IBFD) technology is a promising solution to boost the throughput of wireless networks. To bring IBFD to reality, the modem has to cancel the selfinterference (SI) signal which includes the strong direct Tx leakage and the weaker reflected Tx signal from the surroundings. Adaptive analog and digital SI cancellation schemes have been proposed. It becomes then interesting to understand, though, how the echoed SI could be exploited for enabling radar functionality while reusing the waveform and the already-existing hardware. This paper formulates the mono-static radar system model starting from the communication system model. Beside simulation-based assessment, the performance is also evaluated by an IBFD system prototype which consists of both analog and digital SI canceller modules, enabling >85 dB Tx-Rx isolation. The system is enhanced with Doppler radar functionality, reusing as much as possible the existing IBFD functional blocks. The experimental result shows the accuracy of the proposed system to measure the velocity of mobile objects at various speeds between 0.2 - 1 m/s, while the device is simultaneously served as a node to perform in-band bi-directional communication. This ability suits the proposed system for a broad spectrum of opportunistic remote sensing applications, such as body and hand gesture detection.

*Index Terms*—In-band full-duplex, self-interference cancellation, mono-static Doppler radar, wireless sensing, opportunistic remote sensing, hand and body gesture detection.

## I. INTRODUCTION

TODAY, the use of radios is continuously increasing in commercial and industrial electronic devices and has caused the congestion of the available radio spectrum. This motivates implementing multiple functionalities in such a way that they share the same frequency band and potentially the same hardware platform. A good example is opportunistic radio frequency (RF) sensing, which has been studied extensively to offer a promising alternative to traditional sensing solutions, such as video surveillance and wearable sensors that do not respect users' privacy and comfort.

In opportunistic wireless sensing technology, the already existing electromagnetic waves are reused to extract the environmental context. Such an approach enables a wide range of applications like localization, e-healthcare, through-the-wall tracking, and body and hand gesture recognition. Via embedding the latter capability into smartphones, for instance, the users can go beyond touchscreens by interacting with the device through gestures in the space around it.

There is a substantial body of literature in which the received signal strength indicator (RSSI) of the ambient Wi-Fi signal has been adopted as a metric to perform indoor

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localization [1], [2] and passive human activity/gesture recognition [3]–[6]. Since the temporal and spatial variance can quickly distort the RSSI criteria [7], the recent attempts have focused on extracting the Doppler/velocity, mostly in the form of passive bi-static Doppler radar. In such a scheme, the radar correlates the received signal from the line-of-sight of the source of opportunity (reference signal) with the echo from the target (surveillance signal).

Multiple wireless devices are required to establish a passive bi-static Doppler radar system. The introduced sensing system in [8] enables human gesture recognition by employing multiple Wi-Fi transmitters and one surveillance receiver. Similar works are represented in [9]–[12], which also need a Wi-Fi access point (AP) and a dual-channel receiver. To improve radar performance, the authors in [13] make use of GPS-based clock synchronization to synchronize the reference and the surveillance radios. In [14], a directional coupler and two directional antennas are employed to reduce the requirements to one receiver and one Wi-Fi AP.

There are two fundamental constraints in these prior art opportunistic remote sensing techniques:

- The performance of bi-static passive radars is often sensitive to the isolation of the reference and surveillance channels. Beam antennas have been used to overcome this issue while it narrows the system angle of view (AOV).
   To extend the AOV, multiple directional surveillance receivers have to be employed [13]. This, consequently, increases the realization cost and implementation complexity.
- The transmitted signal in the scenarios mentioned above has a non-continuous nature. Thus, in addition to the clock synchronization between the reference and the surveillance receivers, a second mechanism is required to synchronize the transmitter of opportunity and the bistatic radar. For example, a synchronization technique is presented in [10] to deal with the noncontinuity of the Wi-Fi signal and to reduce the impact of the large beacon interval.

In [15] we addressed the issues mentioned above by introducing a radar-capable Tx-Rx architecture, in which the already existing components of the in-band full-duplex (IBFD) communication platform are reused to perform wireless sensing simultaneously. This approach does not suffer from the sensitive process of over-the-air reference signal reconstruction and facilitates explicit synchronization between the radar illuminator and the surveillance receiver. We also introduced a proof of concept prototype in [16], in which an analog self-interference (SI) isolation circuitry is employed to allow

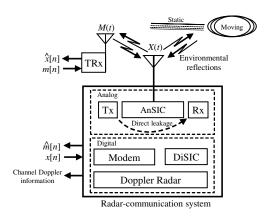


Fig. 1. Overview of the proposed radar-capable IBFD communication device. While the transmit signal X(t) carries information to the other party, the IBFD device can also opportunistically make use of the environmental reflections of X(t) to extract the Doppler state of the channel.

mono-static Doppler detection via processing the environmental echoes of the self-transmit communication signal. Below we outline the contributions of this work that extend our previous studies in [15] and [16] to further enhance the sensing performance in a real-world IBFD communication link.

## A. Contributions

Fig.1 shows the proposed radar-communication (RadCom) system operating in a full-duplex mode where it forms an inband bi-directional link with another communication terminal, shown by the TRx block. As shown, the system benefits from an analog self-interference cancellation (AnSIC) module that provides sufficient Tx-Rx isolation, which is necessary before digital sampling. In addition, a digital self-interference cancellation (DiSIC) unit is embedded in the system. The key contributions in this work are summarized as follows.

- First, we write the mono-static IBFD Doppler radar system model starting from the IBFD communication model. We expand the model in [15] and [16] by deriving a detailed mathematical model, including both analog and digital subsystems. The model determines the narrowband Doppler signal and identifies the different interference components. Via simulations, measurements and analysis, we show that the self- and environmental signal interference for a joint radar and communication system can be resolved.
- Second, we implement an IBFD platform that achieves larger than 85 dB SI rejection, jointly by analog and digital modules, and enables in-band bi-directional communication. Our design also utilizes the DiSIC block to improve the radar by further suppression of the direct SI signal. To this end, we enhance the prototype in [16] by a real-time DiSIC realization, showing that the static analog and hybrid digital filtering enables simultaneous communication and radar functionality for a range of communication distances and Doppler detection speeds.
- Finally, we study the impact of the adaptive analog and digital SI cancellation. The experimental analysis

shows that dynamic tuning of the SI cancellers can remove the Doppler information from the received SI. Hence, the analog and digital SI cancellation coefficients should remain unchanged during the epoch over which the Doppler signal is computed. As this epoch is typically long compared to a channel coherence time, it is not efficient to fix the coefficients from the communication point of view. We, however, show that it is possible to keep the analog SI cancellation static, while having static and dynamic filters for the digital SI cancellation.

The remainder of the paper is structured as follows. Section II briefly introduces the IBFD technology. In Section III, we develop the mathematical system model followed by distortion analysis focusing on the first contribution. The system is then simulated in Section IV giving insight in the joint analog and digital SI cancellation that is needed to get a sufficient SNR for the Doppler signal. For contribution 3, we focus on the analog and digital SI cancellation schemes that are implemented in our SDR prototype, as discussed in Section V. The experimental results are demonstrated in Section VI. Section VII discusses the system limitations and some practical aspects, and finally the conclusion is drawn.

## II. Self-interference Challenge in IBFD Communication

The IBFD technology is well-known for its potential to duplicate the link throughput as it allows transmission and reception over the same frequency band and at the same time. In fact, this is not the only benefit with IBFD since it also allows the device to recapture the environmental reflections of what it transmits. From this point of view, an IBFD radio can be seen as an integrated radar illuminator and receiver.

There are two interfering replicas of the self-transmit signal; a) the analog direct-path leakage shown by the dashed arrow in Fig. 1, and b) the signal reflecting off device-extrinsic scatters, i.e., the static and moving objects in the vicinity.

The direct SI signal is orders of magnitude stronger than the desired low-power signal coming from a remote communication node, to exemplify,  $104\ dB$  in a typical Wi-Fi scenario [17]. This can dramatically reduce the reception sensitivity, or more likely saturates the receiver chain. To enable communication in an IBFD scheme, therefore, the interfering signal has to be suppressed nearly to the noise floor.

To overcome this challenge, typical IBFD architectures make use of an AnSIC block, which guarantees adequate Tx-Rx isolation prior to analog-to-digital conversion (ADC). Once the baseband received signal is digitized, further SI suppression is possible in an additional stage by a DiSIC module.

A real-world IBFD realization has not been possible without the recent advances in SI cancellation technology. The represented active AnSIC techniques in [18], [19], for instance, allow for up to  $70\ dB$  SI cancellation at the RF stage. On the digital side, the authors in [20], [21], suggest a scheme in which they establish a non-linear adaptive design to model the impact of the multipath channel and the hardware imperfections. Their proposed approach estimates the residual

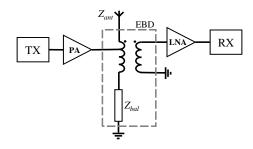


Fig. 2. Structure of a typical EBD-based AnSIC. High SI rejection can be achieved by the electrical balancing of the antenna impedance  $Z_{ant}$  and the dummy load  $Z_{bal}$ .

SI after analog SI attenuation and enhances the sensitivity by subtracting a correction signal from the received baseband signal.

## A. Electrical Balance Duplexing

An electrical balance duplexer (EBD) is a kind of AnSIC scheme which offers impressive linearity and insertion loss performance. In contrast with the non-tunable counterparts, such as fixed-frequency surface-acoustic wave filters, this AnSIC technique allows for scaling and frequency flexibility. Furthermore, using silicon-on-insulator technology, the EBD can be optimally deployed on-chip, which appropriates it for mobile wireless platforms. In the proposed design in this work, the EBD is the key enabling element as it can significantly suppress the direct Tx leakage to allow reception of the environmental SI reflection, which is needed for the Doppler radar.

Fig. 2 depicts the topology of a single-ended EBD. This RF SI cancellation concept is based on hybrid transformers providing signal cancellation through the electrical balancing of two impedances: the antenna impedance  $Z_{ant}$  and an onchip dummy load called the balance network  $Z_{bal}$ . Applying the ideal S-parameters of a symmetrical hybrid (i.e., when the transformer tapping ratio is r=1), the Tx-Rx isolation I can be obtained as follows.

$$I = 20 \log_{10} |\Gamma_{ant} - \Gamma_{bal}| - 6.02, \tag{1}$$

where  $\Gamma_{ant}$  and  $\Gamma_{bal}$  are respectively the complex reflection coefficients of the balancing impedance and the antenna impedance, defined as

$$\Gamma_{ant} = \frac{Z_{ant} - R_o}{Z_{ant} + R_o} \text{ and } \Gamma_{bal} = \frac{Z_{bal} - R_o}{Z_{bal} + R_o},$$
(2)

where  $R_o$  is the output load.

From (1) and (2), it can be shown that the impedance balance between  $Z_{ant}$  and  $Z_{bal}$  causes two equivalent copies of the transmit signal that induce to the secondary winding of the hybrid transformer in opposite phase. Theoretically, this mechanism leads to an infinite direct SI rejection [22].

The balance condition, however, is sensitive to the near-field dynamics as they influence the antenna's impedance. Thus, to maintain the Tx-Rx isolation, an adaptive algorithm is needed to track the substantial environmental changes iteratively and tune  $Z_{bal}$  accordingly.

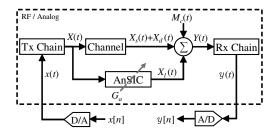


Fig. 3. System model, RF and analog. The received signal Y(t) includes the Tx environmental reflections, while the AnSIC attenuates the direct SI component at the RF front-end by a factor  $G_a$ .

## III. RADAR-CAPABLE IBFD WIRELESS DEVICE

By employing the IBFD technology, the Tx and Rx can operate simultaneously on the same channel, which means the environmental reflections can be recaptured and exploited for remote sensing. From the radar basics, the product of the conjugated transmit signal and the echo from the mobile target yields the Doppler information. However, the received signal in an IBFD communication scheme suffers from two primary sources of interference: a) the distortion caused by a second party transceiver, and b) the direct transmitter leakage.

This section develops the system model for realistic contexts, where there are the above mentioned interfering signals inherent in an IBFD link. Firstly, we describe the RF and analog bandpass signal model. The model is then extended to the digital baseband by representing Doppler radar signal processing in an ideal case, where there is no interference. Then, we explain how the proposed system overcomes the two distortions introduced above.

#### A. System Model, RF and Analog

Fig. 3 depicts the analog subsystem of the proposed Rad-Com device. In this scheme, we adopt capital letters to represent the time-domain RF/analog signals whose baseband equivalents are denoted by the corresponding lowercase letters.

In this model, x(t) is the baseband complex-valued information signal which is indicated by the bandpass communication waveform X(t) after RF up-conversion,

$$X(t) = \Re\{x(t)e^{jw_c t}\},\tag{3}$$

where,  $\Re\{.\}$  denotes the real part of  $\{.\}$  and  $w_c(rad/sec)$  is the frequency of carrier wave.

The static and dynamic environmental reflections of X(t) are also shown by  $X_s(t)$  and  $X_d(t)$  respectively, and the notation  $X_l(t)$  stands for the remaining direct Tx-Rx leakage after the AnSIC block. The desired message arriving at the antenna of the RadCom device is also denoted by  $M_c(t)$ .

As shown in the block diagram in Fig. 3, the received RF signal Y(t) can be expressed as an aggregation of the introduced signals above, i.e.,

$$Y(t) = X_s(t) + X_d(t) + M_c(t) + X_l(t).$$
 (4)

Employing the channel model in [23], we describe the static reflection  $X_s(t)$  as a sum of the echoed signals through a static multipath channel in the form

$$X_{s}(t) = \Re\{\sum_{s \in P_{s}} A_{s} e^{j\varphi_{s}} x(t - \tau_{s}) e^{jw_{c}(t - \tau_{s})}\},$$
 (5)

with  $P_s$  being a set of dominant reflection paths caused by the static objects in the surroundings.  $A_s$  represents the attenuation factor for the  $s^{th}$  path with the initial phase offset  $\varphi_s$  and propagation delay of  $\tau_s$ .

To simplify the model, we assume that there is a single dynamic object in the environment whose acceleration and path loss time-variation are negligible during Doppler estimation. Accordingly, the reflected SI component through the moving object can be written as follows.

$$X_d(t) = \Re\{A_d e^{jw_d t} x(t - \tau_d) e^{jw_c(t - \tau_d)}\},\tag{6}$$

where  $A_d$  denotes the attenuation factor of the dynamic path, and  $w_d$  determines the frequency shift which is linearly influenced by the target velocity.  $\tau_d$  also denotes the propagation delay of the dynamic path.

Similar to the transmit signal from the RadCom device, the received intended message  $M_c(t)$  can be represented as

$$M_c(t) = M(t) * H_c(t) \text{ and } M(t) = \Re\{m(t)e^{jw_c t}\},$$
 (7)

where m(t) is the baseband complex-valued message transmitted by the remote node TRx, M(t) is the RF representation of m(t),  $H_c(t)$  characterizes the medium between the two communication devices, and (\*) is the time-domain convolution operator.

The residual direct Tx leakage after analog SI suppression also can be expressed as

$$X_l(t) = G_a X(t), \tag{8}$$

where  $G_a$  stands for the attenuation factor defining the An-SIC's performance to suppress the direct SI component. Note that the on-chip implementation of the AnSIC block in the presented system allows assuming an insignificant time-delay between  $X_l(t)$  and X(t).

Finally, y(t) in Fig. 3 represents the complex-valued baseband received signal after RF down-conversion. Given the communication signal is bandlimited to  $B\left(Hz\right)$ , the complex-valued discrete-time representation of y(t) after baseband analog to digital conversion is

$$y[n] = y(t = \frac{n}{f_s}) \text{ and } f_s \ge B, \tag{9}$$

with  $f_s$  being the baseband sampling frequency and the integer n denotes the discrete sample index.

## B. Interference-free Doppler Detection

Fig. 4 illustrates the digital part of the presented RadCom system. This subsection explains how the Doppler signal can be extracted from the environmental reflections of the modulated communication signal, while there is no interference from the direct SI leakage and no concurrent transmission by a second party node.

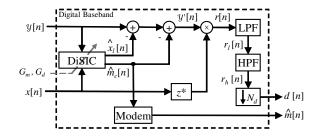


Fig. 4. System model, digital baseband. While the DiSIC block is necessary for in-band bi-directional communication, it also can be employed to suppress the radar-related interference.

Let define the complex baseband information signal x[n] in terms of time-varying magnitude and phase, i.e.,

$$x[n] = A_x[n]e^{j\varphi_x[n]}, (10)$$

where  $A_x[n]$  and  $\varphi_x[n]$  determine the amplitude and phase modulations respectively.

The ideal baseband received signal in the absence of the interfering sources can be defined as

$$y_o[n] = x_s[n] + x_d[n],$$
 (11)

where,  $x_s[n]$  and  $x_d[n]$  are the static and dynamic environmental reflections respectively, both are represented in the sampled baseband. Subsequently, using the equations (5) and (6) they can be written in the form

$$x_s[n] = \sum_{s \in P_s} A_s e^{j\varphi_s} x[n - n_s] \text{ and } n_s = \lfloor \tau_s f_s \rfloor, \qquad (12)$$

and

$$x_d[n] = A_d e^{jw_d n} x[n - n_d] \text{ and } n_d = |\tau_d f_s|,$$
 (13)

where  $|\{.\}|$  is the greatest integer less than or equal to  $\{.\}$ .

In the next step,  $y_o[n]$  is correlated with the conjugated transmit signal x[n]. In the context of the RadCom system, this operation reduces the impact of the phase modulation of the communication signal, i.e.,  $\varphi_x[n]$ . Employing the definitions in (10-13) we define the interference-free radar signal as

$$r[n] = y_o[n]x^*[n] = (x_s[n] + x_d[n])x^*[n]$$
  
=  $\eta_s[n] + A_d e^{jw_d n} x[n - n_d]x^*[n],$  (14)

where  $(.)^*$  is the complex conjugate of (.), shown by  $z^*$  in Fig. 4, and  $\eta_s[n]$  is the distortion caused by the static reflections which can be derived to be

$$\eta_s[n] = \sum_{s \in P_s} A_s e^{j\varphi_s} x[n - n_s] x^*[n].$$
(15)

In practice, the required sample rate for communication is an order of magnitude larger than the highest Doppler frequency. For example, the maximum velocity in hand gesture detection and vehicular applications ranges from  $1\ m/s$  up to  $200\ Km/h$ , which causes a 16 to  $890\ Hz$  Doppler frequency shift to the traditional  $2.4\ GHz$  WiFi signal. This implies that the Doppler information lies in a small portion of the

communication bandwidth. To enhance the radar sensitivity, thus, the signal r[n] has to be severely decimated.

A narrow low-pass filter can be efficiently realized in practice by a moving average filter. Besides, by exploiting the ergodic property of communication signals, it can be shown that the arithmetic average approximates the expected value [24]. Hence, via employing a moving average filter (shown by the LPF block in Fig. 4) we derive the low-pass filtered radar signal in the form

$$r_{l}[n] = \hat{\mathbb{E}}\{r[n]\}\$$

$$= \hat{\mathbb{E}}\{\eta_{s}[n]\} + \hat{\mathbb{E}}\{A_{d}e^{jw_{d}n}x[n - n_{d}]x^{*}[n]\},$$
(16)

where  $\hat{\mathbb{E}}\{.\}$  determines the estimated expected value of  $\{.\}$  which can be computed over  $N_f$  successive realizations of the signal as defined in (17).

$$\hat{\mathbb{E}}\{.\} = \frac{1}{N_f} \sum_{N_f} \{.\}$$
 (17)

Typically, it is desirable to remove the strong DC component of the radar signal until the non-zero Dopplers can be easily visualized in the ultimate Doppler profile. To this end, our model exploits a DC-blocker filter  $h_h[n]$ , shown by the HPF block in the diagram, to suppress the influence of the static reflections in (16), i.e., the term  $\hat{\mathbb{E}}\{\eta_s[n]\}$ . Given that the target motion is statistically independent of the term  $x[n-n_d]x^*[n]$ , and the Doppler component is in the passband of the low-pass filter, we derive the DC-removed radar signal  $r_h[n]$  in the form

$$r_h[n] = r_l[n] * h_h[n] = \hat{\mathbb{E}} \{ A_d e^{jw_d n} x[n - n_d] x^*[n] \}$$
  
=  $A_d \hat{\mathbb{E}} \{ x[n - n_d] x^*[n] \} e^{jw_d n}$ . (18)

Note that for the moving objects in the range  $R < \frac{c}{2B}$  (c is the speed of the light in (m/s)), where  $\hat{\mathbb{E}}\{x[n-n_d]x^*[n]\} \approx \hat{\mathbb{E}}\{x[n]x^*[n]\}$ , one can approximate  $r_h[n]$  as

$$r_h[n] \simeq A_d \hat{P}_x e^{jw_d n},\tag{19}$$

where the term  $\hat{P}_x = \hat{\mathbb{E}}\{A_x^2[n]\}$  denotes the estimated power of the transmit signal x[n].

To accomplish the decimation and to facilitate frequency analysis, the DC-removed radar signal  $r_h[n]$  is down-sampled to obtain the narrow band Doppler signal d[n] as

$$d[n] = r_h[nN_d], (20)$$

where, given the baseband sample rate  $f_s$  and the decimation factor  $N_d$ , d[n] streams at  $f_s/N_d$ .

Using Fast Fourier Transform (FFT), we can analyze d[n] to yield its dominant frequency component, i.e. the Doppler frequency  $f_d = \frac{w_d}{2\pi}$ , and the instantaneous radial target velocity (relative to the radar) v (m/s):

$$f_d = 2\frac{v}{c}f_c,\tag{21}$$

where  $f_c = \frac{w_c}{2\pi}$  is the carrier frequency in Hz. Subsequently, the velocity resolution  $v_{res}$  and the maximum detectable velocity  $v_{max}$  can be determined as follows.

$$v_{res} = \frac{1}{2} \frac{c}{f_c} \frac{f_s}{N_d N_{fft}},\tag{22}$$

$$|v| < v_{max} = \frac{1}{4} \frac{c}{f_c} \frac{f_s}{N_d},$$
 (23)

with  $N_{fft}$  being the number of samples used to obtain the FFT, and |.| denotes the absolute value of  $\{.\}$ .

It is worthwhile to mention that, regarding the application conditions discussed earlier, the system is also applicable to the multi-carrier waveforms, e.g., OFDM, as the imposed Doppler shifts to the orthogonal sub-carriers are nearly identical in such a way that the resultant Doppler signal is a superposition of multiple co-frequency Dopplers.

## C. Doppler Extraction in Presence of Distortion Sources

As described earlier, in an IBFD scenario the received signal also includes the interference signals:

$$y[n] = y_0[n] + m_c[n] + x_l[n],$$
 (24)

where  $y_o[n]$  is the interference-free received signal introduced in (11),  $m_c[n] = M_c(t = \frac{n}{f_s})$  denotes the received intended message in the digital baseband, and  $x_l[n]$  stands for the residual Tx leakage which can be defined according to its analog equivalent in (8) as

$$x_l[n] = X_l(t = \frac{n}{f_c}) = G_a x[n].$$
 (25)

While the DiSIC block is necessary for communication, the proposed system also applies it to enhance the radar. As shown in Fig. 4, the estimated residual direct SI  $\hat{x}_l[n]$  and the estimated message  $\hat{m}_c[n]$  are subtracted from the interfered received signal y[n] defined in (24). Accordingly, the enhanced received signal y'[n] (see Fig.4) can be derived to be

$$y'[n] = y[n] - \{\hat{m}_c[n] + \hat{x}_l[n]\}$$

$$= y_o[n] + m_c[n] - \hat{m}_c[n] + x_l[n] - \hat{x}_l[n]$$

$$= y_o[n] + G_m m_c[n] + G_d x_l[n],$$
(26)

where  $G_m$  determines the performance of DiSIC to attenuate the interference caused by the received desired message  $m_c[n]$ , and  $G_d$  characterizes the DiSIC's capability to reduce the remaining direct SI leakage  $x_l[n]$ . Note that the estimated signal  $\hat{m}_c[n]$  is also fed into the communication modem to extract the message  $\hat{m}[n]$ .

The interfered radar signal then can be defined as

$$r[n] = y'[n]x^*[n].$$
 (27)

To aid our derivations and to facilitate the analysis of the distortions, we rewrite the non-ideal low-pass filtered radar signal  $r_l[n]$  in terms of the two introduced interferences and the Doppler information as follows.

$$r_{l}[n] = \hat{\mathbb{E}}\{r[n]\}$$

$$= \hat{\mathbb{E}}\{(y_{o}[n] + G_{m}m_{c}[n] + G_{d}x_{l}[n])x^{*}[n]\}$$

$$= \hat{\mathbb{E}}\{y_{o}[n]x^{*}[n]\} + \hat{\mathbb{E}}\{\eta_{m}[n]\} + \hat{\mathbb{E}}\{\eta_{l}[n]\},$$
(28)

where  $\eta_m[n]$  denotes the distortion produced by the received desired message  $m_c[n]$ ,  $\eta_l[n]$  represents the distortion introduced by the residual direct SI leakage  $x_l[n]$ , and the term  $\hat{\mathbb{E}}\{y_o[n]x^*[n]\}$  comprises the Doppler information as explained in the interference-free case in the previous part.

## D. Distortion Analysis

1) The interference from the desired received message  $\eta_m[n]$ : as shown in (26), by minimizing  $G_m$ , the DiSIC block can suppress the impact of a probable concurrent in-band transmission on the radar signal.

More importantly, in a real-world IBFD communication scheme, the two transmit signals are likely orthogonal, i.e.,  $\mathbb{E}\{m_c[n]x^*[n]\}=0$ . This allows to approximate the filtered  $\eta_m[n]$  from (28) as

$$\hat{\mathbb{E}}\{\eta_m[n]\} = G_m \,\hat{\mathbb{E}}\{m_c[n]x^*[n]\} \approx 0.$$
 (29)

2) The distortion from the remaining direct Tx leakage  $\eta_l[n]$ : regarding the equations (10), (25) and (28), the interference from the residual SI can be derived to be

$$\hat{\mathbb{E}}\{\eta_{l}[n]\} = \hat{\mathbb{E}}\{G_{d}x_{l}[n]x^{*}[n]\} 
= \hat{\mathbb{E}}\{G_{a}G_{d}x[n]x^{*}[n]\} = G_{l}\hat{P}_{x}.$$
(30)

where  $G_l = G_a G_d$  is the joint analog and digital direct Tx leakage rejection.

Similar to the DC term caused by the static reflection in (16), it is already clear that the DC-removal filter will also suppress the distortion  $\eta_l[n]$ . However, further attenuation is required as the direct Tx leakage is orders of magnitude stronger than the reflected signal from the target, i.e.,  $x_d[n]$ . As shown in (30), the analog and digital SI cancellers directly influence this distortion in such a way that by improving the direct Tx-Rx isolation, i.e.,  $G_l \rightarrow 0$ , the RadCom system can effectively lessen  $\eta_l[n]$ , without affecting the environmental reflections which are needed for Doppler extraction.

# E. Minimum Detectable Velocity as a Function of AnSIC Tuning Rate

In the non-ideal SI cancellation scheme, the EBD has to be re-tuned frequently to maintain sufficient analog SI rejection. Practically, triggering the adaptation algorithm is followed by a random phase shift to the received signal. The EBD tuning rate  $f_{tune}$  hence limits the minimum detectable velocity  $v_{min}$  as the EBD should be stable during the segment used for deriving the Doppler spectrum. Therefore, the duration of the segment, determined by the sample rate, decimation factor and FFT size should be limited which means  $f_{tune} \leq \frac{f_s}{N_d N_{fft}}$ . Combining this with (22) we can define the minimum velocity that remains detectable, i.e.,

$$|v| \ge v_{min} = \frac{1}{2} \frac{c}{f_c} f_{tune}.$$
 (31)

TABLE I IEEE 802.11p-like OFDM Waveform Characteristics

Param.	Value	Param.	Value
strength	20 dBm	OFDM subcarriers	52
bandwidth	10 MHz	OFDM pilots	4
bit rate	6 Mbps	modulation	QPSK

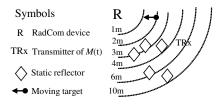


Fig. 5. Layout of the simulated multipath channel.

## IV. SIMULATION RESULTS

In this section, we simulate the proposed RadCom system in the presence of the interfering sources. The simulation aims to: a) evaluate the impact of SI cancellation on the radar, b) investigate the radar performance in an IBFD communication scenario, and c) study the effectiveness of using the DiSIC module to remove the interference caused by a second party transmitter. To this end, we chose an OFDM waveform for both the self-transmit signal x[n] and the message m[n], applying parameters as specified in Table I for IEEE 802.11p. Fig. 5 illustrates the simulated scenario where five motionless reflectors are positioned within  $3-10\ m$  around the radarenabled IBFD device to resemble an indoor multipath channel. A mobile target is also involved in the simulation to produce the Doppler frequency shift, and the transceiver TRx is located at  $6\ m$ .

The simulation is carried out by Matlab in double precision floating-point, the in-band thermal noise is assumed to be -90~dBm and the IBFD receiver samples at 40~MHz. The transmit signals (x[n] and m[n]) are modulated by two statistically independent and zero-mean random data streams. To obtain the interfered radar signal defined in (28), the simulator computes the baseband received signal y[n] taking into account the defined terms in (12), (13) and (25). The decimated and DC-removed Doppler signal d[n] is then estimated at 610 Hz (decimation factor  $N_d=2^{16}$ ), and windowed (Hanning) to be analyzed by FFT. Assuming an observation window of 1000~ms for a transmit signal at 2.4~GHz RF band, this configuration enables up to 18.42~m/s speed measurement with velocity resolution of 6.04~cm/s.

Fig. 6 shows the power spectrum of the low-pass filtered and down-sampled components of the radar signal in (28), without applying the DC-removal filter. In this test, the total SI rejection is set to be  $G_l = -40~dB$ , and a target in 2 m from the radar moves at 5 m/s. Note that despite 40~dB Tx-Rx isolation the distortion  $\eta_l[n]$  is still the dominant interference. In this graph, the non-zero component at 81.4~Hz indicates the Doppler frequency shift, which is relatively less than the DC components caused by the static reflections and the residual

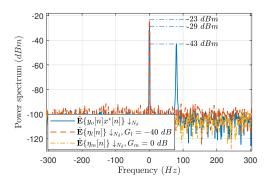


Fig. 6. Power spectrum of the decimated (low-pass filtered and down-sampled by the factor  $N_d=2^{16}$ ) components in (28) without DC-removing, including the distortion of the direct SI  $\eta_l[n]$ , the interference from the desired communication message  $\eta_m[n]$ , and the ideal radar signal, i.e.,  $y_o[n]x^*[n]$ .

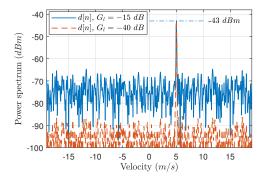


Fig. 7. Power spectrum of the estimated Doppler signal d[n] versus velocity (m/s) as a function of the total Tx leakage rejection  $G_l$ , assuming the target is located at  $d_t = 2$  m from the IBFD device and moves at v = 5 m/s.

direct leakage  $x_l[n]$ . Furthermore, note that the distortion caused by TRx, i.e., the term  $\eta_m[n]$ , is as week as the noise level, even though there is no compensation by the DiSIC module  $(G_m=0\ dB)$ .

## A. Radar Performance Evaluation

In the next step, we repeat the test for 15 and  $40\ dB$  direct SI isolation to evaluate the impact of the direct Tx leakage. This time, the enhanced received signal y'[n] in (26) is feed to the radar mixer. The resultant Doppler signal, after low-pass filtering, DC-removing and down-sampling is also shown in Fig. 7. Note that in this graph, the frequency axis (x-axis) is mapped to velocity by applying the definition in (21). As shown, decreasing  $G_l$  improves the signal-to-noise ratio (SNR) of the detected Doppler signal as it significantly suppresses the impact of the direct Tx leakage. Furthermore, the graph in Fig. 7 shows a  $-43\ dBm$  Doppler component at  $5\ (m/s)$  for both SI rejection levels.

Regarding the simulation results mentioned above, we adopt the SNR of the resultant Doppler signal  $SNR_d$  as a metric to assess the radar performance. To this end, the power of the Doppler component (relative to the noise floor) is computed in the range of  $\pm 2v_{res}$  around the expected target velocity.

Fig. 8 depicts the estimated  $SNR_d$  for different levels of Tx leakage rejection. From this figure, it is obvious that

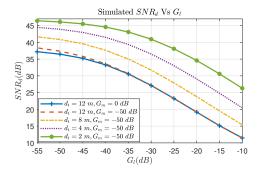


Fig. 8. Simulated SNR of the Doppler signal  $(SNR_d)$  versus the joint analog and digital Tx leakage rejection  $G_l$ , as a function of the distance between the target and the RadCom device  $(d_t)$ , with and without compensation for the interfering message  $m_c[n]$ , i.e.,  $G_m = -50 \ dB$  and  $G_m = 0 \ dB$ .

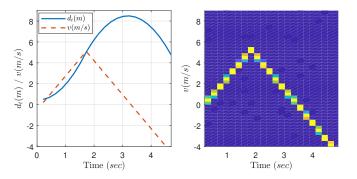


Fig. 9. (Left) Distance and the radial speed of the simulated target, i.e.,  $d_t$  and v respectively. (Right) Estimated Doppler profile of a target moving in a simulated scenario.

decreasing  $G_l$  improves the quality of the Doppler signal in all cases. Moreover, the results reveal that the system offers higher performance as the target approaches the IBFD radio and the system captures stronger reflections.

As explained in the system model representation, the orthogonality of the transmit signals nullifies the distortion caused by a concurrent transmission. Still, it is interesting to assess the effectiveness of the digital cancellation of the intended message on radar performance. Fig. 8 also shows the performance when the DiSIC module provides no compensation  $(G_m=0\ dB)$  for the received message  $m_c[n]$  (the case with  $d_t=12\ m$ ). This proves that given x[n] and  $m_c[n]$  are indeed orthogonal, the interference from the desired signal is insignificant on the Doppler estimation performance.

## B. Doppler Profile

The simulation proceeds by moving the target at different velocities. As illustrated in Fig. 9 (Left), the target firstly moves away from the device at constant acceleration. At  $4.4\ m$ , it decreases the speed until it stops at  $8.5\ m$  and returns toward the device with the same acceleration. The Tx-Rx direct isolation is set to  $50\ dB$  to provide constant SI rejection along with the simulation. Fig. 9 (Right) illustrates the estimated Doppler profile, which precisely follows the ground-truth curve at the left.

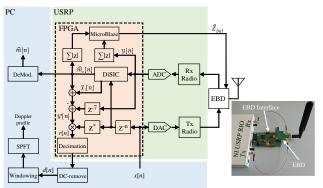


Fig. 10. Block diagram (Left) and the picture (Right) of the prototyped RadCom system.

## V. RADAR-CAPABLE IBFD PROTOTYPE

Fig. 10 (Left) illustrates the functional schematic of the prototyped device whose picture is shown in Fig. 10 (Right). To the best of our knowledge, it is the first demonstration of EBD-based mono-static Doppler radar which is integrated into an IBFD platform and enables simultaneous communication and opportunistic wireless environment sensing.

The implemented system consists of one SDR, one customized EBD-based AnSIC module [19] and one PC. The SDR is a NI USRP RIO with a Kintex-7 FPGA onboard. The EBD is interfaced with the USRP by two 25 cm RF cables and a GPIO bus. The RF cables connect the EBD and the USRP's radio front-end. The whole setup can be controlled and monitored via a PCI-e connection and a LabVIEW user interface. Regarding the EBD's maximum tolerable RF input and its operating frequency band, the power of the OFDM signal is limited to -8 dBm and the USRP's RF front end is tuned to 1.74 GHz. We also use an omnidirectional antenna as such the device can radiate/receive to/from all directions and maintain its communication functionality. To synchronize the Tx-baseband to Rx-baseband signals, the model employs a n-tap delay block shown by  $z^{-n}$  in the block diagram. By connecting the EBD's antenna port to a 50  $\Omega$  dummy load, we measured the delay n=119 samples in our prototype. The USRP produces 60 MHz complex baseband signal which has to be mixed with the transmitted signal. Prior to the mixer, the estimated signals  $\hat{m}_c[n]$  and  $\hat{x}_l[n]$  are subtracted from the received signal. A 7-sample delay block is also embedded to compensate for the latency with the digital SI canceller. The mixed signal is then decimated to achieve narrow-band complex signal with a configurable rate in the range of 457 to 1828~Hz. The real-time processing on the FPGA is in 16bit and 32-bit fixed-point precision and, as shown in Fig. 10, the rest of the computation is accomplished on a computer to build up a 2-D Doppler profile. Theoretically, this configuration enables detecting targets moving up to  $78.73 \, m/s$  with  $8.6 \ cm/s$  speed resolution (for one second observation time).

## A. EBD Tuning Implementation

The EBD tuner in our system is deployed on the MicroBlaze softcore [25] which enables real-time adaptation within  $0.125\ ms$ . As shown in the prototype schematic, the

```
Algorithm 1: EBD Tuner
```

```
Input: Hadamard sequence H_{N\times 4}, convergence factor \mu
Result: Maximize analog Tx-Rx isolation aiming I>I_{th}
```

1 Initialize:  $Z_{bal} = zeros(1,4), \ n=0$ 2 while  $I < I_{th}$  do 3  $\mid \delta = H(n,:)$ 

4  $I = \text{MeasureIsolation}(Z_{bal} + \delta)$ 

5  $Z_{bal} = Z_{bal} - \mu (I - I')^2 \delta$ 6  $I' = \text{MeasureIsolation}(Z_{bal})$ 

n = Reminder(n+1, N)

instantaneous SI is observed through feedback from the EBD receiver port. Based on the level of the measured SI, the tuner adjusts the impedance network adaptively, seeking to maximize the Tx-Rx isolation. The  $Z_{bal}$  in the prototyped EBD comprises four adjustable capacitors, each can obtain  $2^8$  distinct capacitance values. In this work, the dithered linear search (DLS) algorithm [26], presented in Algorithm 1, is adopted to explore a 4-dimension solution space, finding the optimum point where the analog SI isolation I is better than a certain threshold  $I_{th}$ .

The DLS algorithm is a gradient descent optimizer in which signals with small amplitude and zero-mean, the dither sequences  $\delta$ , are intentionally injected into the impedance network parameters, i.e.,  $Z_{bal} = \{c_1, c_2, c_3, c_4\}$ . The additive independent and uncorrelated dither signals allow multiple duplexer parameters can be updated concurrently. The dithers are generated by Hadamard sequences in our implementation.

Once the EBD is initialized, the tuner also measures the level of the estimated  $\hat{m}_c[n]$  by the DiSIC block. This mechanism guarantees appropriate residual SI measurement in the full-duplex communication mode.

## B. Digital Self-interference Canceller Implementation

On top of analog SI rejection, digital cancellation is also needed to achieve sufficient SNR required for communication as well as to improve the radar performance. The digital SI canceller in this work models both linear and nonlinear impacts of the physical circuitry and the channel. The DiSIC block is based on an adaptive spline-based Hammerstein model consisting of a spline-interpolated lookup table cascaded with an adaptive linear filter [27], [28]. The former model matches the static nonlinearities and the latter tracks the linear part of the SI signal. This configuration closely resembles the physical system and the most influential source of nonlinear distortion, the transmitter power amplifier and the linear SI channel. Fig. 11 illustrates the basic Hammerstein DiSIC mode which is briefly summarized below. For a complete description, including derivations and equations, we refer the reader to [28].

As shown in Fig. 11, the baseband transmit signal x[n] is fed to the spline model, which produces the spline estimate s[n] using a lookup table  $\mathbf{q}_n$  and a second-order spline interpolator.

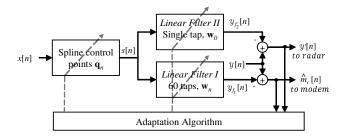


Fig. 11. Adaptive spline-based Hammerstein model used for digital self-interference cancellation. While the multi-tap filter can estimate the remaining SI signal, the single tap filter merely computes the residual direct Tx leakage without affecting the environmental SI echoes.

Then, a 60-tap linear filter, shown by Linear Filter I, produces the cancellation signal  $y_{f_1}[n]$ , that is the estimate of the direct Tx leakage and the environmental SI reflections, i.e.,  $y_{f_1}[n] = \hat{x}_l[n] + \hat{x}_s[n] + \hat{x}_d[n]$ . The estimated SI is subtracted from the received signal to yield  $\hat{m}_c[n]$ , which is required to perform communication. While removing the environmental Tx reflections requires an adaptive filter with multiple taps, it can be shown that a single tap filter is sufficient to suppress the residual direct Tx leakage merely. Accordingly, a single tap filter, demonstrated by the Linear Filter II block, is embedded to generate the cancellation signal  $y_{f_2}[n] = \hat{x}_l[n]$ .

The DiSIC block exploits a standard least-mean squares (LMS) optimizer [29] to update the adaptive filter parameters dynamically. This algorithm utilizes the signals  $\hat{m_c}[n]$  and y'[n] as feedback to converge to the optimum state. To achieve real-time functionality, the DiSIC is fully implemented on the FPGA. The 60-tap filter implementation consists of 533 DSP units, each of which can handle up to 25  $\times$  18-bit multiplications. The same FPGA realization allocates 67632 LUTs. The DiSIC block has seven pipeline stages with seven clock cycles latency and provides up to 40~dB Tx-Rx isolation. In our implementation, *Linear Filter I* is tuned every eight samples while the system adjusts *Linear Filter II* at the same rate as the EBD.

## VI. EXPERIMENTAL RESULTS

This section details the experimental results obtained by the system prototype. First, the required EBD tuning rate is measured in an indoor environment. Second, the SI rejection performance is shown and finally, we assess the accuracy and the performance of the velocity estimation experimentally.

## A. EBD Tuning Trade-off

In Section II, we discussed the necessity of EBD retuning and introduced  $f_{tune}$  as a parameter which limits the minimum detectable velocity. In this part, we investigate  $f_{tune}$  in an indoor environment. Fig. 12 displays the cumulative distribution functions of the EBD isolation, measured in a typical office room where the device is placed on a desk next to a working person at  $0.5\ m$ . In each experiment, an isolation threshold is specified to trigger the EBD tuning algorithm. The level of the SI signal and the number of triggers are recorded for 60 minutes to estimate how often the EBD has to be tuned

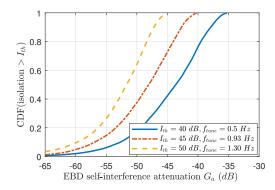


Fig. 12. Empirical cumulative distribution function (CDF) plot of the EBD isolation performance versus various tuning thresholds  $I_{th}$ , measured in an indoor environment.

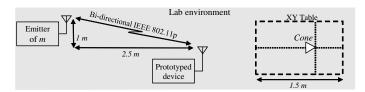


Fig. 13. Schematic of the testbed. Two IBFD devices are used to form an IBFD link, and a XY positioner moves a cone reflector at various velocities.

to maintain the Tx-Rx isolation below the threshold. Note that the actual achieved isolation depends on the EBD setting and the environment, giving a distribution of instantaneous isolation values. Each time the EBD is retuned, a more optimal configuration for the given environment is determined. It is evident that increasing the isolation threshold raises the required EBD tuning speed and, consequently, increases the minimum detectable velocity expressed by (31). According to the experimental results in Fig. 12, to obtain  $50\ dB$ ,  $45\ dB$  and  $40\ dB$  analog SI cancellation, the EBD requires respectively  $1.3\ Hz$ ,  $0.93\ Hz$  and  $0.5\ Hz$  tuning rates. These tunning frequencies limit  $v_{min}$  to 0.11, 0.80 and  $0.43\ m/s$  respectively.

## B. Doppler Measurement

To evaluate the radar capability of the prototyped device, a remotely controlled XY table is utilized to move a cone reflector with radar cross-section (RCS)  $-17\ dBsm$  at different speeds ranging from 0.2 to  $1\ m/s$ , as shown in Fig. 13. Due to the omnidirectionality of the antenna, the system is also exposed to statistic reflections from a lab environment. Another communication device is also placed at  $2.7\ m$  from the prototype to enable IBFD communication. The radios transmit packets starting with IEEE 802.11ac header, followed by a random bitstream.

Fig. 14 shows the Doppler profile obtained by short-time Fourier transform (STFT), when the reflector moves forward and backward at different velocities. Each segment in this spectrogram is 500~ms, including 85% overlap with the adjacent frame. Due to inertia in the mechanical setup, there is a visible artifact in the spectrogram when the target changes the direction.

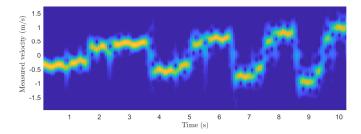


Fig. 14. Measured Doppler profile produced by the prototyped device representing the movement of a mounted cone reflector on a XY table which moves at  $\pm 0.4$ ,  $\pm 0.6$ ,  $\pm 0.8$  and  $\pm 1$  m/s. STFT segment 500 ms with 85% overlap, Doppler signal at 915 Hz, Hanning window, 8k-point FFT,  $G_I < -45$  dB.

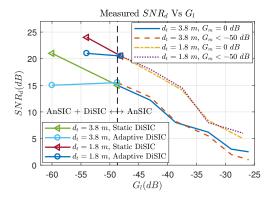


Fig. 15. Measured  $SNR_d$  versus the total Tx leakage rejection  $G_l$  as a function of the target distance from the radar  $d_t$ , when a moving reflector at 1.8 m and 3.8 m moves at 0.3 m/s and the radar transmits a -8~dBm IEEE 802.11p-like waveform at 1.74 GHz. The static analog SI cancellation improves the radar performance. Similarly, the single tap filter of the DiSIC module should remain unchanged otherwise it does not enhance the radar sensitivity.

Fig. 15 shows the measured  $SNR_d$  when the reflector is located at  $1.8 \, m$  and  $3.8 \, m$  from the radar. As indicated by the vertical dashed line in this graph, up to  $48 \, dB$ Tx-Rx isolation is provided only by the AnSIC block. As expected, the measured result in this experiment proves that the static analog SI cancellation by the EBD suppresses the SI sufficiently enough to enable both communication and Doppler detection. Furthermore, better Doppler quality is achievable for the objects closer to the radar. For further Tx-Rx isolation, the DiSIC module is also utilized. This graph also shows that the SI rejection is increased when DiSIC adaptively tunes the single tap filter. However, this adaptive digital filter does not improve  $SNR_d$  as it partially cancels the Doppler as well. We also observed that a filter with eight adaptive taps can thoroughly remove the Doppler. Combining static and dynamic digital filters, thus, improves both communication and radar performance.

To evaluate the impact of the DiSIC compensation for  $m_c[n]$  on radar performance in full-duplex mode, the measurement also has been done with and without subtracting the estimated communication signal  $\hat{m}_c[n]$  from the received signal, i.e.  $G_m < -50 \; dB$  and  $G_m = 0 \; dB$  respectively. As illustrated in Fig. 15, this experiment verifies that the impact of the interference from another emitter in full-duplex communication mode is insignificant, even when the two transmitted information

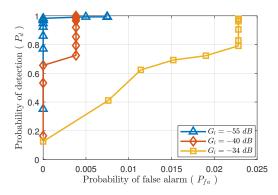


Fig. 16. Measured  $P_d$ - $P_{fa}$  graph for different levels of direct SI rejection and the target moves at  $0.2\ m/s$ .

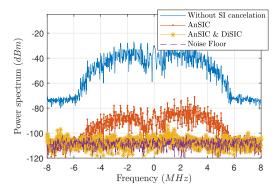


Fig. 17. Measured power spectrum of the received signal, with and without SI cancellation. Joint analog and digital modules are required to enable in-band bi-directional communication.

packets, x[n] and  $m_c[n]$  in this case for example, carry the same header.

Fig. 16 presents the performance in terms of the probability of correct velocity detection  $(P_d)$  and the likelihood of false alarm  $(P_{fa})$ . For each measurement in this figure, the reflector moves (forward and backward) five times at the speed of  $0.2\ m/s$ . The measurements are performed for various levels of EBD SI cancellation. Then, the spectrogram is formed and the most significant FFT component is chosen to compute the target velocity. Next, the estimated speed is compared with the ground-truth. By changing the detection thresholds, various probabilities are measured. Regarding the results in Fig. 16, increasing the direct SI suppression improves the likelihood of correct velocity detection.

## C. SI Rejection for Communication

Fig. 17 demonstrates the measured power spectrum of the received OFDM signal, including the direct and environmental SI components. This graph shows how the combination of AnSIC and DiSIC modules in our prototype can suppress the SI signal to the noise level, allowing bi-directional communication. We measured the average bit error rate of the IBFD link < 1.5% at both sides in the testbed shown in Fig. 13.

## VII. DISCUSSION

In contrast with the classic mono-static radars, there are some constraints imposed by the simultaneous communication functionality of the proposed RadCom system. First of all, the radar relies on the Tx communication signal, and hence, cannot sense when the Tx is idle. One approach to resolve it is to simply interpolate between the sensing periods. Another possible approach is to add a bi-static radar functionality to also benefit from the presence of other Tx signals. The majority of the required hardware is already available for that purpose.

Besides, since the communication standards primarily dictate the operation bandwidth, it seems inefficient to add the range detection functionality for low-bandwidth communication links. Furthermore, to decode a low-SNR communication signal in a highly dynamic environment, the system has to increase the tuning rate of the analog SI canceller. Consequently, it restricts the minimum detectable velocity of the radar since the observation time is reduced in that case.

#### VIII. CONCLUSION

This paper presents an IBFD radar-communication system that enables joint communication and opportunistic wireless sensing, and to the author's knowledge, is the first of its kind. Our solution can be built into future IBFD devices without extra hardware deployment. In this work, we study how various interfering sources influence the performance of the radar. The proposed system is evaluated using an IEEE 802.11p-like waveform and a prototyped device, consisting of an EBDequipped SDR. The implemented digital SI canceller benefits from a 60-tap adaptive filter which, jointly with the EBD, delivers  $> 85 \, dB$  SI rejection required for communication. A single tap digital filter that has to be tuned regarding the EBD's adaptation rate is also utilized to enhance the radar signal further. We conclude that this adaptation rate limits the minimum detectable velocity. The proof-of-concept prototyped system in this work can precisely measure velocities in the range of  $0.2-1 \ m/s$  while the device establishes an in-band bi-directional link with another IBFD device.

According to the simulation and experimental results, the radar performance is mainly dependent on the extent of direct SI cancellation. Whereas, in full-duplex mode, the distortion caused by an adjacent communication device is negligible as long as both transmit signals are uncorrelated.

More work is needed to derive system specifications, in terms of system bandwidth, symbol and packet length, etc., that are suitable both for radar and communication systems. Moreover, the proposed RadCom system could in the future be equipped with an antenna array to further estimate the signal direction of arrival.

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