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UNIVERSITÉ LIBRE DE BRUXELLES  
AERO-THERMO-MECHANICS

# Dynamics of Gas Jet Impinging on Falling Liquid Films

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