Photoneutron cross sections for Mo isotopes: A step toward a unified understanding of \((\gamma,n)\) and \((n,\gamma)\) reactions

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Photoneutron cross sections were measured for \(^{94}\)Mo, \(^{95}\)Mo, \(^{96}\)Mo, \(^{97}\)Mo, \(^{98}\)Mo, and \(^{100}\)Mo near the neutron threshold with quasi-monochromatic laser-Compton scattering \(\gamma\) rays. The photoneutron data were analyzed with the Skyrme Hartree-Fock-Bogolubov (HFB) plus quasiparticle random phase approximation (QRPA) model and the axially symmetric-deformed Gogny HFB plus QRPA model of \(E1\) \(\gamma\)-ray strength. Combining the \(\gamma\)-ray strength function constrained by the present photoneutron data with either the nuclear resonance fluorescence data or the updated Oslo data to supplement the data below the neutron threshold, a thorough analysis of the reverse \((n,\gamma)\) cross sections is made whenever measurements are available. The Oslo data and the corresponding uncertainties are updated based on the latest results of the \(s\)-wave neutron spacing and the average radiative width determined in particular for \(^{96}\)Mo. Finally, radiative neutron capture cross sections for two radioactive nuclei, \(^{99}\)Mo and \(^{99}\)Mo, are deduced with the \(\gamma\)-ray strength function method.

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I. INTRODUCTION

Photoneutron cross sections and radiative neutron capture cross sections are fundamental nuclear inputs to stellar model calculations of the \(s\), \(r\), and \(p\)-process nucleosynthesis. A comprehensive understanding of \((\gamma,n)\) and \((n,\gamma)\) cross sections requires a knowledge of nuclear statistical quantities such as the \(\gamma\)-ray strength function \((\gamma\text{SF})\) and the nuclear level density. The \(\gamma\text{SF}\) is the quantity which interconnects photoneutron emission and radiative neutron capture, thus, is a key to the Hauser-Feshbach model calculations of both \((n,\gamma)\) and \((\gamma,n)\) cross sections. As discussed in [1,2], the \(\gamma\text{SF}\) plays an important role in both nuclear astrophysics and nuclear engineering. Photoneutron cross sections, hence the \(\gamma\text{SF}\), immediately above neutron threshold is of direct relevance to the production and destruction of \(^{94}\)Mo, \(^{95}\)Mo, \(^{96}\)Mo, \(^{97}\)Mo, \(^{98}\)Mo, and \(^{100}\)Mo among which those for two odd-\(N\) isotopes, \(^{95}\)Mo and \(^{97}\)Mo, are presented here for the first time. We systematically discuss \((\gamma,n)\) and \((n,\gamma)\) cross sections for molybdenum isotopes in the context of the \(\gamma\)-ray strength function \((\gamma\text{SF})\) method [1,2]. The photoneutron emission and radiative neutron capture on Mo isotopes of interest in the present paper are depicted in Fig. 1. The neutron thresholds even for the two odd-\(N\) nuclei were not low enough to directly detect extra low-energy strength in the photoneutron channel. However, combining the \(\gamma\text{SF}\) constrained by the present data with the low-energy data derived from either the \((\gamma,\gamma')\) [9,10] or the Oslo [8] experiments (updated with the latest results of the \(s\)-wave resonance spacing and the average \(\gamma\)-decay width [12]) enables us to analyze \((n,\gamma)\) cross sections for stable Mo isotopes systematically. The photoneutron data and the \(\gamma\text{SF}\) for \(^{95}\)Mo and \(^{94}\)Mo are of direct relevance to the production and destruction of \(^{94}\)Mo, respectively, in the \(p\)-process nucleosynthesis though there is a well-known issue of the underproduction of \(^{92}\)Mo and \(^{96}\)Mo in this mass region of the chart of nuclei [3]. With the \(\gamma\)-ray strength function method, we indirectly determine \((n,\gamma)\) cross sections for two radioactive Mo isotopes, \(^{93}\)Mo with the half-life \(4 \times 10^3\) yr and \(^{98}\)Mo with the half-life 2.75 d, which constitute nuclear inputs for the reaction network calculations for the \(p\) and \(s\) process, respectively.

II. PHOTONEUTRON CROSS SECTION MEASUREMENTS

The experiment was performed with quasi-monochromatic laser-Compton scattering (LCS) \(\gamma\) rays at the National Institute of Advanced Industrial Science and Technology (Japan).
The present measurement for molybdenum isotopes was made in parallel to that for tin isotopes [13] in the same experiment. Therefore, we restrict ourselves to the description of the experimental procedure specific to the measurement for molybdenum isotopes, while other details can be found in Refs. [1,13].

The LCS $\gamma$ rays were produced in an energy range from 7.55 MeV to 13.00 MeV (the quoted energy represents the maximum energy of the LCS $\gamma$-ray beam) with a high-intensity Nd:YVO$_4$ Q-switch laser. Enriched metal powders of $^{94}$Mo (98.97%, 1921 mg), $^{95}$Mo (94.38%, 1992 mg), $^{96}$Mo (95.9%, 2001 mg), $^{97}$Mo (91.7%, 999 mg), $^{98}$Mo (98.55%, 1749 mg), and $^{100}$Mo (99.27%, 2850 mg) were pressed/shaped into targets of 8 mm diameter and 16–19 mm lengths.

Measurements below the neutron threshold $S_n$ were carried out for $^{94}$Mo ($S_n = 9.68$ MeV) at 9.50 MeV, $^{96}$Mo ($S_n = 9.15$ MeV) at 9.00 MeV, and $^{100}$Mo ($S_n = 8.29$ MeV) at 8.25 MeV with no significant neutron events observed. The LCS $\gamma$-ray beam was measured with the high-resolution high-energy photon spectrometer [14] at a reduced laser power to determine the energy distributions of the LCS $\gamma$-ray beam by means of the unfolding technique [15,16]. Figure 2 shows an example of the unfolded energy spectra of the incident $\gamma$-ray beams.

Photoneutron cross sections were deduced at the average $\gamma$-ray energies with the Taylor expansion method [1]. The systematic uncertainty for the cross section is $\pm 4.4\%$, which represents a quadratic sum of uncertainties of the neutron detection efficiency (3.2%) and the number of incident $\gamma$ rays (3%). The final cross sections are shown in Fig. 3 and compared with previous measurements when available.

III. COMPARISON WITH THEORETICAL PREDICTIONS AND AUXILIARY DATA

The photoneutron cross-section data have been compared to theoretical calculations on the basis of the TALYS nuclear reaction code [19] and two different models of the $\gamma$SF, namely the Skyrme HFB plus QRPA model [20] based on the BSk7 interaction, and the axially symmetric-deformed Gogny HFB plus QRPA model based on the D1M interaction [21–23]. Both models are based on the QRPA approach but make use of different interactions. The BSk7 + QRPA model is based on the BSk7 Skyrme force where some phenomenological corrections are introduced to take the damping of the collective motion as well as the deformation effects into account. In contrast to the Skyrme-based model, the D1M + QRPA model allows for a consistent description of axially symmetric deformations and includes phenomenologically the impact of multiparticle multihole configuration as a function of their densities [23]. Both models have proven their capacity to reproduce experimental photoabsorption data relatively well. As seen in Fig. 3, cross sections around the neutron threshold are rather well described by the HFB + QRPA models, although some deviations can be seen. Note that no renormalization of the strength has been performed for these calculations. In contrast to other cases, see for example Ref. [1], the agreement around the neutron threshold is rather satisfactory and there is no reason to invoke the presence of extra low-lying strength from the present data, at least in the vicinity of the neutron threshold.

Below the neutron threshold, additional experimental information exists; this includes the $(\gamma,\gamma')$ measurements on $^{92,94,96,98,100}$Mo [10,24], and the analysis of particle-$\gamma$ coincidence data on $^{93–98}$Mo from neutron pickup $(^3$He,$\alpha\gamma$) and/or inelastic scattering $(^3$He,$^3$He$'$\gamma$) reactions [8,25]. As shown in Figs. 4 and 5, such measurements cover a rather large range of energies below the neutron threshold. However, the shape and absolute value of the $\gamma$SF from the two measurements seem to be contradictory. One should keep in mind that both methods are affected by rather large model-dependent uncertainties, although those might not be reflected in the quoted error bars, which typically show statistical errors only. It is interesting to note that for $^{95}$Mo, the overall shape of the $\gamma$SF extracted with the Oslo method is in excellent agreement with recent $(d,p\gamma)^{95}$Mo data from Ref. [26].

![FIG. 2. A typical energy distribution of the LCS $\gamma$-ray beam used in the present experiment.](image-url)
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FIG. 3. (Color online) Comparison between the present photoneutron emission cross sections and previously measured ones [17,18] for six Mo isotopes, $^{94}$Mo $^{(a)}$, $^{95}$Mo $^{(b)}$, $^{96}$Mo $^{(c)}$, $^{97}$Mo $^{(d)}$, $^{98}$Mo $^{(e)}$, and $^{100}$Mo $^{(f)}$. Also included are the predictions from Skyrme HFB + QRPA (based on the BSk7 interaction) [20] and axially deformed Gogny HFB + QRPA models (based on the D1M interaction) [23].

To determine the $\gamma$SF within the Oslo method, data on the s-wave resonance spacing $D_0$ and the average total radiative width $\langle \Gamma_1 \rangle$ from neutron-resonance experiments are essential for the normalization procedure (see Ref. [27] for a more detailed description of the method, and Ref. [28] for a thorough analysis of possible systematic errors). In the original normalization [8], the values recommended by the RIPL library [29] were considered. However, a detailed analysis of a new $^{95}$Mo($n, \gamma$) $^{96}$Mo measurement [12,30] shows a significant deviation from the RIPL $D_0$ and $\langle \Gamma_1 \rangle$ values, more specifically $D_0$ is reduced by 63% and $\langle \Gamma_1 \rangle$ is increased by 25%. The corresponding error bars are rather small (see Table I) due to the large number of resonances available in the new experiment. Since such a detailed analysis is not available for the other Mo isotopes, we assume that the corresponding RIPL $D_0$ and $\langle \Gamma_1 \rangle$ values are affected by similar uncertainties. For this reason, we have adopted a similar uncertainty range for the other Mo isotopes for which Oslo data are available, as summarized in Table I.

Those uncertainties are responsible for the large error bars shown in Figs. 4 and 5, especially when the $D_0$ value is not well constrained. Note that the error bars shown in these figures include statistical uncertainties for the Oslo data sets and uncertainties in the $D_0$ and $\langle \Gamma_1 \rangle$ values.

Regarding the $(\gamma,\gamma')$ data [10,24], the systematic errors are not so transparent. However, considering uncertainties due to the applied level density models as shown in Fig. 17 of Ref. [10], the systematic error is at least a factor of 2. In addition, there are possible systematic errors due to assumptions of the input $\gamma$SF model and the equal-parity distribution applied in the correction procedure to estimate missing quasicontinuum strength.

Finally from Figs. 3–5, it can be seen that even if there is no reason to invoke the presence of some extra strength above the neutron threshold with respect to the QRPA predictions, below the threshold, some pygmy resonances, as observed for example for the Sn isotopes [13], may still be required to explain the $(\gamma,\gamma')$ data, in particular in $^{94,96,98}$Mo. The D1M + QRPA model systematically predicts larger $E1$ strength below the neutron threshold than the BSk7 + QRPA one and is also seen to be in better agreement with data in this energy region.

IV. RADIATIVE NEUTRON CAPTURE AND THE $\gamma$SF METHOD

We now turn to the reverse radiative neutron capture channel. It should be kept in mind that the corresponding cross section for incident keV neutrons depends sensitively on the $\gamma$SF, but in a rather lower energy range below the neutron threshold, typically around 6 MeV of $\gamma$-ray energy.

On the basis of the $\gamma$-ray strength shown in Figs. 4 and 5, i.e., either the Oslo data or the $(\gamma,\gamma')$ data, both supplemented by the Gogny HFB plus QRPA predictions [21,23] outside the measured range, the reverse radiative neutron capture cross sections are now estimated with the TALYS reaction code [19] and compared with experimental cross sections.
FIG. 4. (Color online) Comparison between the measured photoabsorption cross sections derived from photoneutron experiments (including ours) [17,18] as well as particle-γ coincidence measurements [8,25] (see also text for the corresponding error bars) and (γ,γ') data [24] for three Mo isotopes, 94Mo (a), 96Mo (b), and 98Mo (c). Predictions from Skyrme HFB + QRPA (based on the BSk7 interaction) [20] and axially deformed Gogny HFB + QRPA models (based on the D1M interaction) [23] are also included.

in Fig. 6. In addition to the E1 strength function which, in the energy range of relevance here, is essentially taken from experimental data, the TALYS calculation also depends on the adopted nuclear level density. We have used here the HFB plus combinatorial model of Ref. [34] normalized to exactly the same D0 value and corresponding error bars, as those used to determine the γ SF from the Oslo data (see Table I). Note that no uncertainty analysis has been performed when use is made of the (γ,γ') data, the systematic experimental error bars being most probably underestimated, as discussed above.

As can be seen in Fig. 6, the TALYS calculation agrees well with experimental data, which shows that within the uncertainties affecting the experimental γ SF and D0 value, all γ SF data are compatible with both the photoabsorption and radiative capture channels, despite the fact that, as shown in Fig. 4, discrepancies exist between the different measurements. In the 95Mo(n,γ)96Mo, the larger 96Mo γ SF determined by photon scattering clearly leads to larger neutron capture cross sections.

The γ SF method can now be applied to the experimentally unknown cross sections, namely 93Mo(n,γ)94Mo and 99Mo(n,γ)100Mo. While experimental information exists on the E1 strength function, no experimental D0 data at the neutron binding energy can guide the nuclear level density models. For this reason, different D0 values are adopted for 94Mo, as given in Table I, and different level density models [35,36] considered to estimate their impact on the final cross section. Considering uncertainties affecting the experimental γ SF (see Figs. 4 and 5) and theoretical ones affecting nuclear level densities, we have estimated the final upper and lower limits of the cross sections, as shown in Fig. 7. For the 99Mo(n,γ)100Mo cross section, the error bars only rely on the (γ,γ') data (with relatively small error bars) since there has been no particle-γ coincidence measurements yet for 100Mo; this explains why smaller error bars are found in this case.

The resulting cross sections are also compared with the Japanese JENDL-4.0, American ENDF/B-VII.1, and Russian ROSFOND-2010 evaluations [37] in Fig. 7. While our 99Mo(n,γ)100Mo estimate is in good agreement with previous evaluations, our 93Mo(n,γ)94Mo cross section clearly does not

TABLE I. Adopted range of values for the average resonance spacings D0 (in eV) and average γ -width (Γγ) (in meV).

<table>
<thead>
<tr>
<th>Nucleus</th>
<th>D0&lt;sub&gt;min&lt;/sub&gt;</th>
<th>D0&lt;sub&gt;max&lt;/sub&gt;</th>
<th>(Γγ)&lt;sub&gt;min&lt;/sub&gt;</th>
<th>(Γγ)&lt;sub&gt;max&lt;/sub&gt;</th>
</tr>
</thead>
<tbody>
<tr>
<td>94Mo</td>
<td>81</td>
<td>105</td>
<td>123</td>
<td>149</td>
</tr>
<tr>
<td>95Mo</td>
<td>83</td>
<td>108</td>
<td>169</td>
<td>118</td>
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<td>96Mo</td>
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<td>69.1</td>
<td>188</td>
<td>186</td>
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<tr>
<td>97Mo</td>
<td>661</td>
<td>859</td>
<td>138</td>
<td>96</td>
</tr>
<tr>
<td>98Mo</td>
<td>47</td>
<td>53</td>
<td>163</td>
<td>130</td>
</tr>
</tbody>
</table>
agree with the Russian evaluation despite the non-negligible error bars. The resulting Maxwellian-averaged cross sections of astrophysical interest amount, at 30 keV, to 380 ± 200 mb for $^{93}\text{Mo}(n,\gamma)^{94}\text{Mo}$ and 410 ± 130 mb for $^{99}\text{Mo}(n,\gamma)^{100}\text{Mo}$. Our $^{99}\text{Mo}(n,\gamma)^{100}\text{Mo}$ estimate (and consequently, also the ENDF/B-VII.1 and JENDL-4.0 ones) is found to be significantly larger than the theoretical cross sections of 240 ± 40 mb recommended in Ref. [38].

V. CONCLUSION

We have completed a systematic measurement of photoneutron cross sections for stable Mo isotopes with $A = 94–100$ using quasi-monochromatic laser-Compton $\gamma$-ray beams. In the context of the $\gamma$SF method, we have investigated the $\gamma$-ray strength function that interconnects ($\gamma,n$) and ($n,\gamma$) cross sections within the statistical reaction model. We get a reasonable agreement with the experimental photoneutron and radiative neutron-capture cross sections for the Mo isotopes, using the Gogny HFB + QRPA model of $E1$ strength supplemented with experimental data that have been obtained by photon scattering or particle-$\gamma$ coincidence data from ($^{3}\text{He},\alpha\gamma$) and ($^{3}\text{He},^{3}\text{He}\gamma$) reactions.

The new and accurate determination of the $s$-wave spacing for $^{96}\text{Mo}$ shows that in this specific case, there is a strong coherence between the different measurements, be it for the $\gamma$SF in $^{96}\text{Mo}$ or the photoneutron and radiative neutron-capture cross sections. Some discrepancies are still found between the ($\gamma,\gamma'$) and particle-$\gamma$ coincidence techniques, but accurate $D_0$ and $\langle\Gamma_{\gamma}\rangle$ evaluation at the neutron binding energy may help to resolve such discrepancies and give a coherent picture of the reaction mechanism. The present method shows that it is possible to significantly reduce the uncertainties in the determination of the neutron-capture rates on unstable nuclei if the $\gamma$-ray strength function can be determined experimentally below and in the vicinity of the neutron threshold. This method could consequently improve the predictions relative to the
nuclear physics ingredients of relevance in the description of the branching points in the s-process nucleosynthesis. More implications on nucleosynthesis will be studied in a forthcoming paper.

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